

HOTROCK®

NOTEBOOK

The best quality goods always make you happy.

Antennae

8mm



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15

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21

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$$\vec{A} \times \vec{B} = \vec{C}$$

$$\vec{A} \times \vec{B} = \vec{C}$$

$$0 = (\vec{A} \times \vec{B}) \cdot \vec{C}$$

$$\vec{A} \times \vec{B} = -\vec{C}$$

$$\vec{A} + \vec{B} = \vec{C}$$

$$\vec{A} + (\vec{A} \times \vec{B} - \vec{C}) = \vec{C}$$

$$\vec{A} + \vec{C} = \vec{C}$$

$$0 = \vec{A} \cdot \vec{C}$$

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四版 天线

一. 引言

辐射: 馈电 \rightarrow 空间

接收: 空间 \rightarrow 馈电

二. 辐射场

1. 电流源和磁流源的矢量位

令
$$\vec{H}_e = \frac{1}{\mu} \nabla \times \vec{A}_e \quad ①$$

代入
$$\nabla \times \vec{E}_e = -j\omega \mu \vec{H}_e$$

得
$$\nabla \times (\vec{E}_e + j\omega \vec{A}_e) = 0$$

令
$$\vec{E}_e + j\omega \vec{A}_e = -\nabla \phi_e$$

代入
$$\nabla \times \vec{H}_e = j\omega \epsilon \vec{E}_e + \vec{J}_e$$

得
$$\frac{1}{\mu} \nabla \times \nabla \times \vec{A}_e = j\omega \epsilon (-\nabla \phi_e - j\omega \vec{A}_e) + \vec{J}_e$$

即
$$\nabla^2 \vec{A}_e + k^2 \vec{A}_e = -\mu \vec{J}_e + \nabla (\nabla \cdot \vec{A}_e + j\omega \epsilon \mu \phi_e)$$

洛伦兹规范
$$\nabla \cdot \vec{A}_e + j\omega \epsilon \mu \phi_e = 0$$

得
$$\nabla^2 \vec{A}_e + k^2 \vec{A}_e = -\mu \vec{J}_e \quad ②$$

且
$$\phi_e = -\frac{1}{j\omega \epsilon \mu} \nabla \cdot \vec{A}_e \quad ③$$

代入
$$\vec{E}_e + j\omega \vec{A}_e = -\nabla \phi_e$$

得
$$\vec{E}_e = -j\omega \vec{A}_e - \frac{1}{j\omega \epsilon \mu} \nabla (\nabla \cdot \vec{A}_e) \quad ④$$

解②得
$$\vec{A}_e(\vec{r}) = \frac{\mu}{4\pi} \int \frac{e^{-jk|\vec{r}-\vec{r}'|}}{|\vec{r}-\vec{r}'|} \vec{J}(\vec{r}') dV' \quad ⑤$$

将⑤代入①和④可算出由电流源 \vec{J}_e 产生的电场 \vec{E}_e 和 \vec{H}_e .

令
$$\vec{E}_m = -\frac{1}{\epsilon} \nabla \times \vec{A}_m \quad ⑥$$

代入
$$\nabla \times \vec{H}_m = j\omega \epsilon \vec{E}_m$$

得
$$\nabla \times (\vec{H}_m + j\omega \vec{A}_m) = 0$$

令
$$\vec{H}_m + j\omega \vec{A}_m = -\nabla \phi_m$$

代入
$$\nabla \times \vec{E}_m = -j\omega \mu \vec{H}_m - \vec{J}_m$$

得 $-\frac{1}{\epsilon} \nabla \times \nabla \times \vec{A}_m = -j\omega\mu(\nabla\phi_m - j\omega\vec{A}_m) - \vec{J}_m$
 即 $\nabla^2 \vec{A}_m + k^2 \vec{A}_m = -\epsilon \vec{J}_m + \nabla(\nabla \cdot \vec{A}_m + j\omega\epsilon\mu\phi_m)$

洛伦兹规范 $\nabla \cdot \vec{A}_m + j\omega\epsilon\mu\phi_m = 0$

得 $\nabla^2 \vec{A}_m + k^2 \vec{A}_m = -\epsilon \vec{J}_m$

且 $\phi_m = -\frac{1}{j\omega\epsilon\mu} \nabla \cdot \vec{A}_m$

代入 $\vec{H}_m + j\omega\vec{A}_m = -\nabla\phi_m$

得 $\vec{H}_m = -j\omega\vec{A}_m - \frac{1}{\omega\epsilon\mu} \nabla(\nabla \cdot \vec{A}_m)$

解得 $\vec{A}_m(\vec{r}) = \frac{\epsilon}{4\pi} \int \frac{e^{-jkR}}{R} \vec{J}_m(\vec{r}') dV'$

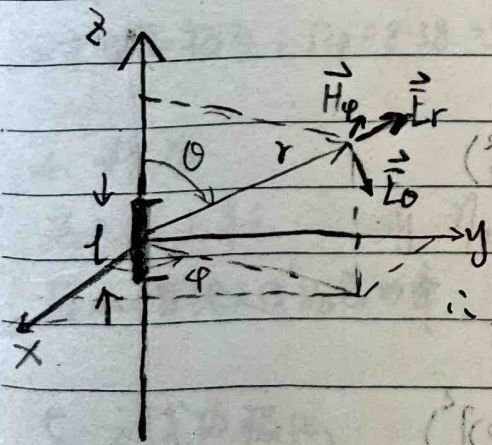
将④代入①和②可算出由磁流源 \vec{J}_m 产生的 \vec{E}_m 和 \vec{H}_m .

2. 电偶极子辐射场

电偶极子：长为 l 沿 z 轴放置的无限小电偶极子。

$$\vec{A}(\vec{r}) = \frac{\mu I l e^{-jkR}}{4\pi r} \hat{z} = A_z \hat{z}$$

$$\begin{cases} A_r = A_z \cos\theta = \frac{\mu I l e^{-jkR}}{4\pi r} \cos\theta \\ A_\theta = -A_z \sin\theta = -\frac{\mu I l e^{-jkR}}{4\pi r} \sin\theta \\ A_\phi = 0 \end{cases}$$



$$\begin{cases} H_\theta = \frac{I l e^{-jkR}}{4\pi r} \left(\frac{jk}{r} + \frac{1}{r^2} \right) \sin\theta \\ E_r = \frac{I l e^{-jkR}}{4\pi r} \left(\frac{2\eta}{r^2} + \frac{2}{j\omega\epsilon r^3} \right) \cos\theta \\ E_\theta = \frac{I l e^{-jkR}}{4\pi r} \left(\frac{j\omega\mu}{r} + \frac{\eta}{r^2} + \frac{1}{j\omega\epsilon r^3} \right) \sin\theta \\ E_\phi = H_r = H_\phi = 0 \end{cases}$$

近区场 $kr < 1$

$$\begin{cases} E_r \approx -j\eta \frac{I l e^{-jkR}}{2\pi k r^3} \cos\theta \\ E_\theta \approx -j\eta \frac{I l e^{-jkR}}{4\pi k r^3} \sin\theta \\ H_\theta \approx \frac{I l e^{-jkR}}{4\pi r^2} \sin\theta \end{cases}$$

远区场 $kr \gg 1$

$$\begin{cases} E_r \approx 0 \\ E_\theta \approx j\eta \frac{k I l e^{-jkR}}{4\pi r} \sin\theta \\ H_\theta \approx j \frac{k I l e^{-jkR}}{4\pi r} \sin\theta \approx \frac{E_\theta}{\eta} \end{cases}$$

由 $\vec{S} = \frac{1}{2}(\vec{E} \times \vec{H}^*) = \hat{r} S_r + \hat{\theta} S_\theta + \hat{\phi} \cdot 0$

得
$$\begin{cases} S_r = \frac{1}{2} E_0 H_0^* = \frac{\eta}{8} \left(\frac{2I}{\lambda}\right)^2 \frac{\sin^2 \theta}{r^2} \left[1 - j \frac{1}{(kr)^3}\right] \\ S_\theta = -\frac{1}{2} E_r H_\phi^* = j\eta \frac{kI^2 \cos \theta \sin \theta}{16\pi^2 r^3} \left[1 + \frac{1}{(kr)^2}\right] \end{cases}$$

总辐射功率
$$P = \oint \vec{S} \cdot d\vec{s} = \int_0^{2\pi} d\phi \int_0^\pi \vec{S} \cdot \hat{r} r^2 \sin \theta d\theta$$

$$= \eta \frac{\pi}{3} \left(\frac{2I}{\lambda}\right)^2 \left[1 - j \frac{1}{(kr)^3}\right]$$

全部为电偶极子辐射功率

$$P_{rad} = \eta \frac{\pi}{3} \left(\frac{2I}{\lambda}\right)^2$$

$$= \frac{1}{2} \left[\eta \frac{2\pi}{3} \left(\frac{I}{\lambda}\right)^2 \right] I^2$$

$$= \frac{1}{2} \left[80\pi^2 \left(\frac{I}{\lambda}\right)^2 \right] I^2$$

三. 天线的基本参数 (一)

1. 中辐射方向图

① 远区场中 \vec{E} 、 \vec{H} 仅有 $\hat{\theta}$ 、 $\hat{\phi}$ 分量

$$\vec{E} = \hat{\theta} E_\theta + \hat{\phi} E_\phi$$

$$\vec{H} = \hat{\phi} E_\theta - \hat{\theta} E_\phi$$

$$\vec{S} = \frac{1}{2}(\vec{E} \times \vec{H}^*) = \hat{r} \frac{1}{2} (|E_\theta|^2 + |E_\phi|^2)$$

② 远区场中为球面波

$$E_\theta = \frac{f_\theta(\theta, \phi)}{r} e^{jkr}$$

$$E_\phi = \frac{f_\phi(\theta, \phi)}{r} e^{jkr}$$

$$\therefore S_r = \frac{1}{2\eta r^2} (|f_\theta(\theta, \phi)|^2 + |f_\phi(\theta, \phi)|^2)$$

功率辐射方向图

$$F(\theta, \phi) = r^2 S_r = \frac{1}{2\eta} (|f_\theta(\theta, \phi)|^2 + |f_\phi(\theta, \phi)|^2)$$

归一化辐射方向图

$$F_n(\theta, \phi) = F(\theta, \phi) / F_{max}(\theta, \phi) = S_r / S_{rmax}$$

对电偶极子

$$F_n(\theta, \phi) = \sin^2 \theta \quad \begin{cases} E \text{ 面} & \phi = \text{const} \\ H \text{ 面} & \theta = 90^\circ \end{cases}$$

2. 天线之体例

定向图立体角

$$\Omega_p = \int_{\Omega_p} F_n(\theta, \varphi) d\Omega$$

主瓣立体角

$$\Omega_m = \int_{\Omega_m} F_n(\theta, \varphi) d\Omega$$

旁瓣立体角

$$\Omega_n = \int_{\Omega_n} F_n(\theta, \varphi) d\Omega$$

3. 方向性

设 P_r 为辐射功率

$$D(\theta, \varphi) = \frac{S_r(\theta, \varphi)}{P_r / 4\pi r^2}$$

若天线无耗

$$= \frac{4\pi S_r(\theta, \varphi) r^2}{P_r}$$

若空间无耗

$$= \frac{4\pi S_r(\theta, \varphi) r^2}{\int_{\Omega} S_r(\theta, \varphi) r^2 d\Omega}$$

$$= 4\pi F(\theta, \varphi) / \int_{\Omega} F(\theta, \varphi) d\Omega$$

$$= 4\pi F_n(\theta, \varphi) / \int_{\Omega} F_n(\theta, \varphi) d\Omega$$

$$= 4\pi F_n(\theta, \varphi) / \Omega_p =$$

$$= D_0 F_n(\theta, \varphi)$$

其中, 最大方向性

$$D_0 = \frac{4\pi}{\Omega_p} \frac{F_n=1}{F_n} D(\theta_0, \varphi_0)$$

对电偶极子, $\Omega_p = 8.38 = \Omega_m$, $D_0 = 1.5$.

4. 增益

若天线无耗

$$\eta_e = \frac{P_r}{P_{in}}$$

P_{in} 为馈给天线的总功率.

5. 天线的极化

最大增益方向 辐射波比极化: 天线的极化

6. 天线的输入阻抗

目的: 天线与馈线 特性阻抗匹配

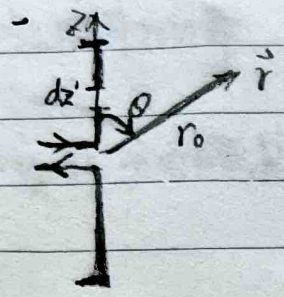
输入电阻: 取决于损耗电阻、辐射电阻

输入电抗: 取决于近区场.

四. 略

五. 振子天线

1. 对称振子



根据电偶极子的辐射场. 远区场

$$dE_{\theta} \approx j\eta \frac{k I(z') e^{-jkr}}{4\pi r} \sin\theta dz'$$

$$\approx j\eta \frac{k I(z') e^{jk(r_0 - z' \cos\theta)}}{4\pi r_0} \sin\theta dz'$$

设 $I(z') \approx \begin{cases} I_0 \sin[k(\frac{l}{2} - z')] & 0 \leq z' \leq \frac{l}{2} \\ I_0 \sin[k(\frac{l}{2} + z')] & -\frac{l}{2} \leq z' < 0 \end{cases}$

得 $E_{\theta} = j\eta \frac{ke^{-jkr_0}}{4\pi r_0} \sin\theta I_0 \int_{-\frac{l}{2}}^{\frac{l}{2}} \sin[k(\frac{l}{2} + z')] e^{jkz' \cos\theta} dz'$

$$+ j\eta \frac{ke^{-jkr_0}}{4\pi r_0} \sin\theta I_0 \int_{-\frac{l}{2}}^{\frac{l}{2}} \sin[k(\frac{l}{2} - z')] e^{jkz' \cos\theta} dz'$$

$$= j\eta \frac{I_0 e^{-jkr_0}}{2r_0} \left[\frac{\cos(\frac{kl}{2} \cos\theta) - \cos(\frac{kl}{2})}{\sin\theta} \right]$$

$H_{\phi} = E_{\theta} / \eta$

$$F_n(\theta, \phi) = \frac{\cos(\frac{kl}{2} \cos\theta) - \cos(\frac{kl}{2})}{\sin\theta}$$

方向图

半波振子: $l = \frac{\lambda}{2}$

$$\begin{cases} E_{\theta} = j\eta \frac{I_0 e^{-jkr_0}}{2\pi r_0} \left[\frac{\cos(\frac{\pi}{2} \cos\theta)}{\sin\theta} \right] \\ H_{\phi} = j \frac{I_0 e^{-jkr_0}}{2\pi r_0} \left[\frac{\cos(\frac{\pi}{2} \cos\theta)}{\sin\theta} \right] \\ F_n(\theta, \phi) = \frac{\cos(\frac{\pi}{2} \cos\theta)}{\sin\theta} \quad \theta = \frac{\pi}{2} \end{cases}$$

$$S_r = \frac{1}{2\eta} |E_{\theta}|^2 = \frac{2\eta I_0^2}{(4\pi r_0)^2} \left[\frac{\cos(\frac{\pi}{2} \cos\theta)}{\sin\theta} \right]^2$$

$$P_{rad} = \int_{\Omega} S_r r_0^2 d\Omega = 0.609 \frac{\eta I_0^2}{2\pi}$$

$$R_{rad} = \frac{P}{I_0^2/2} = \frac{0.609\eta}{\pi} \approx 73\Omega$$

$$Z_{in} \approx R_{rad} = 73\Omega$$

2. 折叠振子

方向性与半波振子相同. $Z_i = 4Z_{\frac{\lambda}{2}} = 292\Omega$. 易与 300Ω 平行或成阻抗匹配.

$$R_{rad} \approx 2Z_{\frac{\lambda}{2}} = 146\Omega.$$

六. 阵列天线

1. 二元阵

$$E_{\theta} = E_{\theta_1} + E_{\theta_2} = j \frac{\eta k I l}{4\pi r} \left[\frac{e^{j(kr_1 - \frac{l}{2})}}{r_1} \sin\theta_1 + \frac{e^{j(kr_2 + \frac{l}{2})}}{r_2} \sin\theta_2 \right]$$

$$\begin{aligned} &\approx j \frac{\eta k L^2}{4\pi r} e^{jkr} \sin\theta \left[e^{j(kd \cos\theta + \beta)/2} + e^{-j(kd \cos\theta + \beta)/2} \right] \\ &= j \frac{\eta k L^2}{4\pi r} e^{jkr} \sin\theta \cdot 2 \cos \frac{kd \cos\theta + \beta}{2} \\ &= j \frac{\eta k L^2}{4\pi r} e^{jkr} f(\theta, \varphi) \end{aligned}$$

2. N元阵列

$$f_a(\psi) = a_0 + a_1 e^{j\psi} + \dots + a_{N-1} e^{j(N-1)\psi}, \quad \psi = kd \cos\theta + \beta$$

当等幅时 $f_a(\psi) = \frac{\sin N\psi/2}{\sin \psi/2}$

归一化 $f_a(\psi) = \frac{1}{N} \frac{\sin N\psi/2}{\sin \psi/2} = Sa(N\psi/2)$

主瓣半最大点: $\psi = 0$

副瓣半零点: $\frac{N\psi_p}{2} = p\pi, \quad p = \pm 1, \pm 2, \dots, \pm \frac{N}{2}$

旁瓣半最大点: $\frac{N\psi_m}{2} = \frac{2p+1}{2}\pi, \quad p = 1, \pm 2, \dots, -\frac{N}{2}$

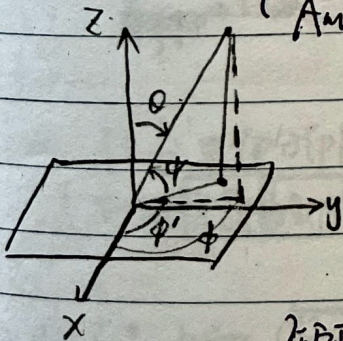
七. 四面天线

$$\begin{cases} \text{对相位: } r \approx r_0 - r' \cos\zeta = r_0 - \vec{r}' \cdot \hat{r} \\ \text{对幅度: } r \approx r_0 \end{cases}$$

$$\begin{cases} \vec{A}_e = \frac{\mu}{4\pi r_0} \int_S \vec{J}_{es} \frac{e^{jkr}}{r} ds' \approx \frac{\mu e^{jkr_0}}{4\pi r_0} \int_S \vec{J}_{es} \cdot e^{jkr' \cos\zeta} ds' \\ \vec{A}_m = \frac{\epsilon}{4\pi r_0} \int_S \vec{J}_{ms} \frac{e^{jkr}}{r} ds' \approx \frac{\epsilon e^{jkr_0}}{4\pi r_0} \int_S \vec{J}_{ms} \cdot e^{jkr' \cos\zeta} ds' \end{cases}$$

$$r' \cos\zeta = \vec{r}' \cdot \hat{r} = x' \sin\theta \cos\varphi + y' \sin\theta \sin\varphi$$

电子体等效 + 镜像原理: $\vec{J}_{ms} = -2\hat{n} \times \vec{E}_a, \quad \vec{J}_{es} = 0$



矩形四面, 均匀场强分布时 $\vec{J}_{ms} = -2\hat{n} \times \vec{E}_a = \hat{x} \cdot 2E_0$

$$\begin{aligned} \vec{A}_m &= \hat{x} \frac{\epsilon E_0}{4\pi r_0} \int_{-a/2}^{a/2} \int_{-b/2}^{b/2} 2E_0 e^{jk(x' \sin\theta \cos\varphi + y' \sin\theta \sin\varphi)} dx' dy' \\ &= \hat{x} \frac{\epsilon E_0}{2\pi r_0} E_0 ab Sa\left(\frac{ka}{2} \sin\theta \cos\varphi\right) Sa\left(\frac{kb}{2} \sin\theta \sin\varphi\right) \end{aligned}$$

$$\therefore E_\theta \approx -j\omega\eta A_{m\varphi} = j \frac{abk\epsilon_0 E_0 e^{jkr}}{2\pi r_0} \sin\varphi Sa\left(\frac{ka}{2} \sin\theta \cos\varphi\right) Sa\left(\frac{kb}{2} \sin\theta \sin\varphi\right)$$

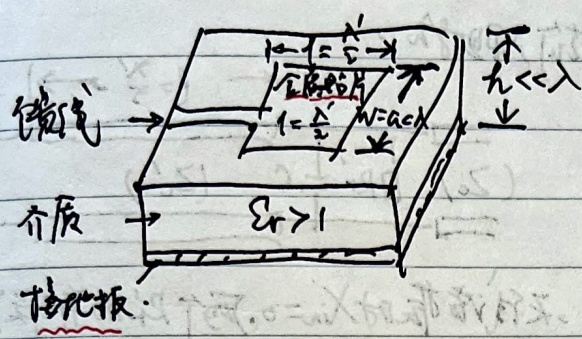
$$E_\varphi \approx -j\omega\eta A_{m\theta} = j \frac{abk\epsilon_0 E_0 e^{jkr}}{2\pi r_0} \cos\theta \cos\varphi Sa\left(\frac{ka}{2} \sin\theta \cos\varphi\right) Sa\left(\frac{kb}{2} \sin\theta \sin\varphi\right)$$

$$H_\theta \approx -E_\varphi/\eta$$

$$H_\varphi \approx E_\theta/\eta$$

13. 微带天线

1. 矩形微带天线结构

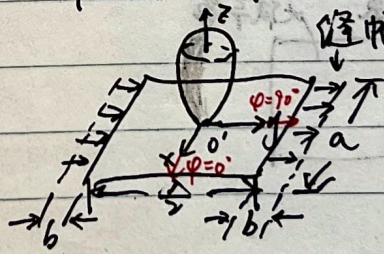
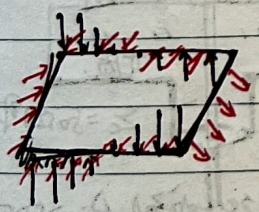


2. 优缺点

- a. 具有平面结构，易于集成，且易于飞行中的表面展开。
- b. 适合于印刷电路技术批量生产。
- c. 易于构成天线阵。
- d. 频带宽，功率容量小，辐射效率高。

3. 矩形微带天线的分析方法和辐射方向图函数：传输线模型理论。

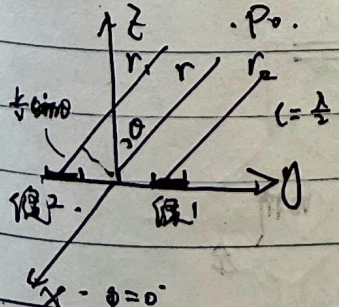
可将单缝看作单天线（辐射源），求二边射线图即可。



$\Gamma = \frac{\lambda}{2}$ 电场分布图
(电场在 Γ 处有分布)

辐射功率分布图。
(其余分量在 $\pm z$ 方向的辐射相互抵消)

$\Delta \phi = 90^\circ$, 侧面 (有波程差 $\frac{\lambda}{2} \sin \theta$)



$$f_{E_{\theta}, \Sigma} = f_{E_{\theta}}(\theta) \cdot f_{a \Sigma} = S_a \left(\frac{k b}{2} \sin \theta \right) \cdot 2 \cdot \cos \left(\frac{k l}{2} \sin \theta \right)$$

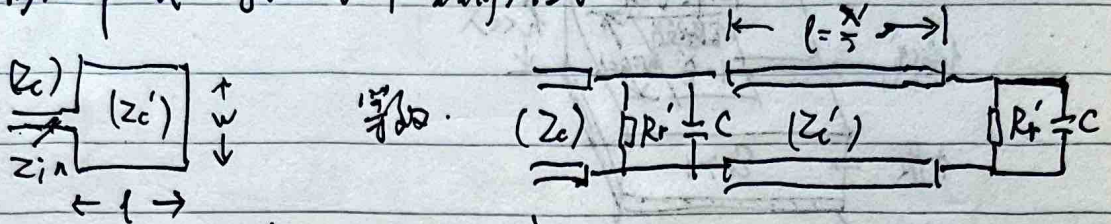
$$= S_a \left(\frac{k b}{2} \sin \theta \right) \cdot 2 \cdot \cos \left(\frac{k l}{2} \sin \theta \right)$$

$$f_{H_{\theta}, \Sigma} = f_{H_{\theta}}(\theta) \cdot 2 = S_a \left(\frac{k a}{2} \sin \theta \right) \cdot 2 \cdot \cos \theta$$

$\Delta \phi = 0^\circ$, 正面 (无波程差，同相位)

4. 等效电路和输入阻抗

A. 对称带状天线的等效电路和输入阻抗



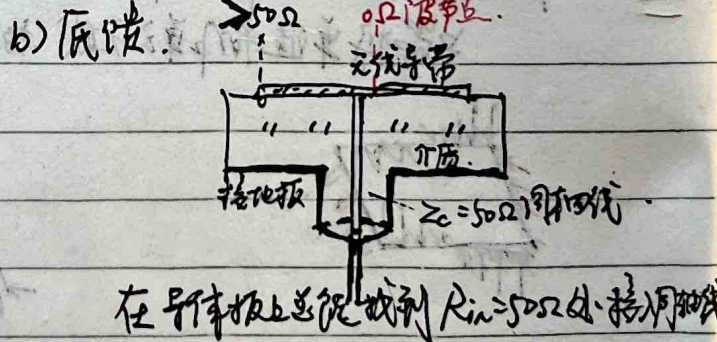
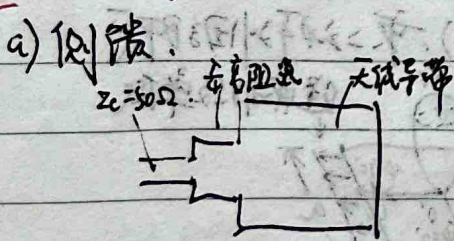
输入阻抗 $Z_{in} = \frac{R_r}{2}$ ($\because l = \frac{\lambda}{2}$, 天线谐振时 $X_{in} = 0$, 两个 R_r 的并联)

研究表明 $R_r \rightarrow R_r'$

$$\begin{cases} R_r \approx 120 \frac{\lambda}{W} \Omega & (W \geq 2\lambda) \\ R_r \approx 90 \left(\frac{\lambda}{W}\right)^2 \Omega & (W < 0.35\lambda) \\ R_r = \frac{1}{W/120\lambda - 1/60\pi^2} \Omega & (0.35\lambda \leq W < 2\lambda) \end{cases}$$

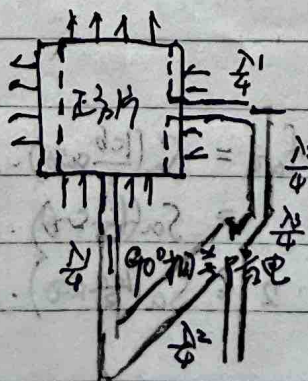
改变 R_r' 可改 W , 改变效率可改 l

5. 馈电方式

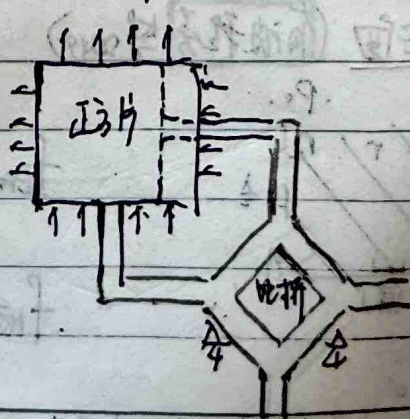


6. 圆极化技术

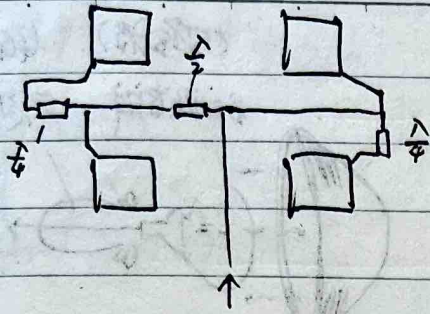
a) 正交支路馈电



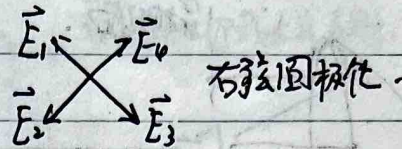
b) 分支线耦合馈电



c)



4单元圆极化天线

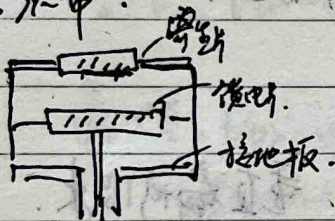


7. 圆极化波的测量方法.

旋转线极化天线测量不同角度的辐射强度.

8. 宽频带、双频带天线.

薄片展宽频带:

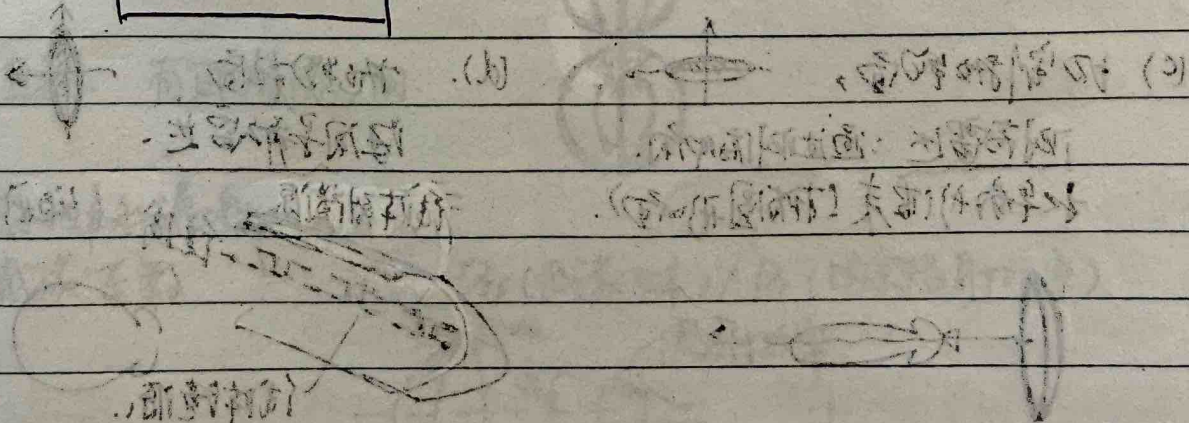
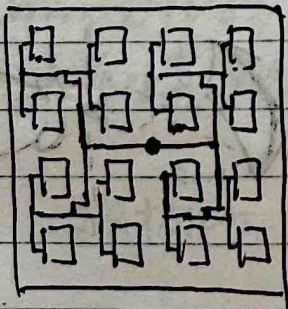


两板展频带相临, 展宽频带.

两板展频带相隔稍远, 则双频带.

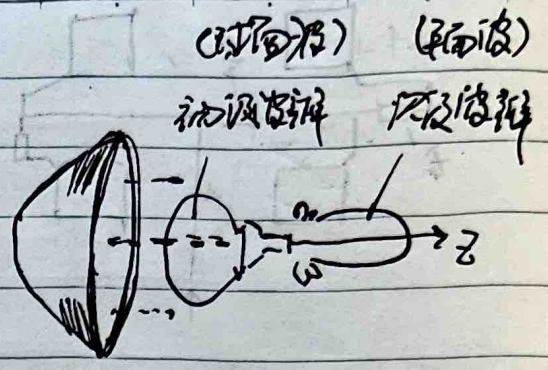
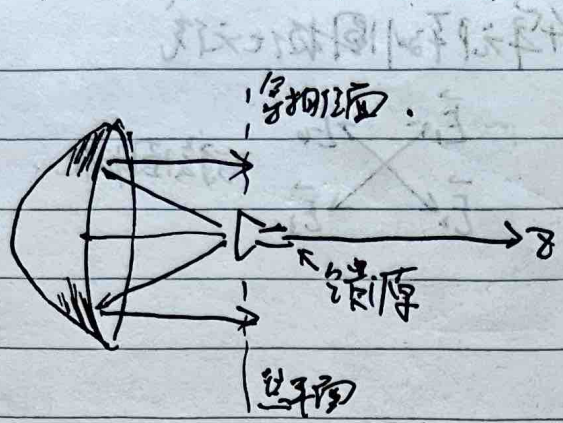
9. 天线阵.

16单元阵列天线, T型馈电并联馈电



§14. 抛物面天线.


1. 引言.

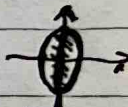


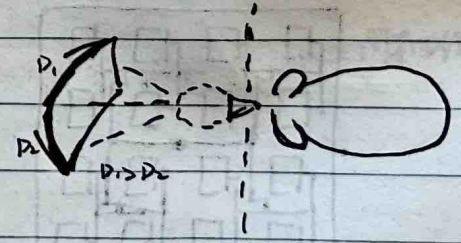
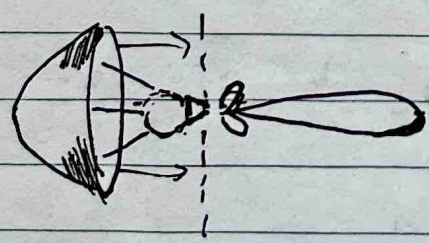
抛物面天线的光学性质: (厘米波段、毫米波段适用).


- ① 反射波平行于轴; 平行于轴的光线入射时聚焦于焦点.
- ② 焦点发出的光线到焦平面的距离都相等, 为 $2f$.


2. 各种形式的抛物面天线.

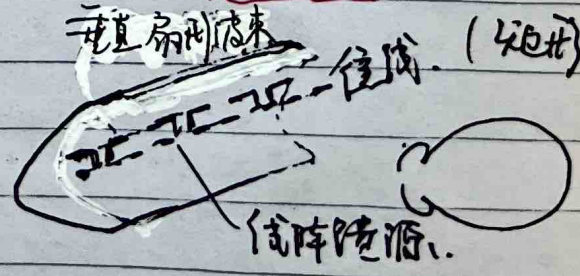
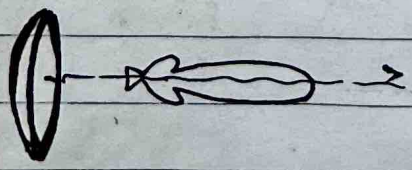
(a) 针状波束. 
跟踪雷达、卫星电话
旋转抛物面天线

(b) 垂直扇形波束. 
警戒雷达、防倾转
切割抛物面(矩形口面).



(c) 切割抛物面, 
测高雷达: 通过测俯仰角.
水平扇形波束(椭圆形口面).

(d). 抛物面柱面 
海用导航雷达.
垂直扇形波束
阵列阵源. (矩形口面).



b, c 常合用

3. 减小风阻和重量的方法.

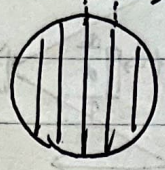
多层栅片结构.



$$\begin{cases} |E| \propto e^{-\alpha x} \\ P \propto e^{-2\alpha x} \end{cases}$$

减小风阻.

\vec{E} :



垂直板对电磁波反射.

波长越短, 孔径越小.

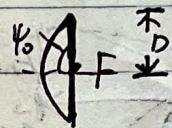


$$a < \frac{\lambda}{2} \Rightarrow a < \frac{\lambda}{4} \left(\frac{\lambda}{10} \sim \frac{\lambda}{20} \right)$$

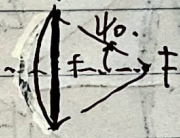
打孔 $\phi < \frac{\lambda}{4}$ ($\frac{\lambda}{10} \sim \frac{\lambda}{20}$)

4. 不同焦距的抛物面天线.

(a) 中焦距 $\psi_0 = \frac{\pi}{2}, f/D = 0.25.$

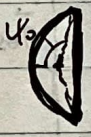


(b) 长焦距. $\psi_0 < \frac{\pi}{2}, f/D > 0.25.$
(0.25 ~ 0.6).



通常电特性好.

(c) 短焦距. $\psi_0 > \frac{\pi}{2}, f/D < 0.25.$



机械特性好.

5. 不同焦距时的口径场分布 (\vec{E}, \vec{H} 分布)

(a) 中焦距. 中心处有交叉极化.



(b) 长焦距. 交叉极化少.



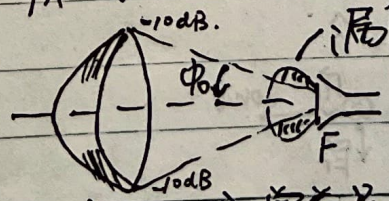
(c) 短焦距. 有反向抵消, 不用.



6. 截获功率和漏射功率.

增益系数

$$\eta_A = P_{rs} (\text{截获功率}) / P_r (\text{天线辐射功率}).$$

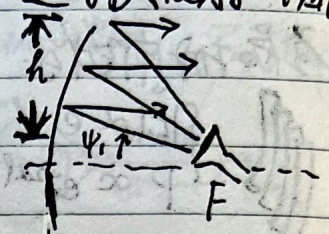
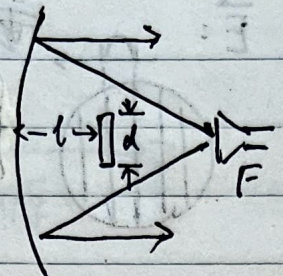
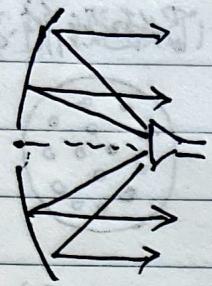


漏射功率.

当边缘带增益射功率为 -10dB 时, 天线增益最大.

7. 互射面的馈源的相互影响及消除办法.

问题: 遮挡、反射入馈源



①. 抛物面馈源开圆孔.

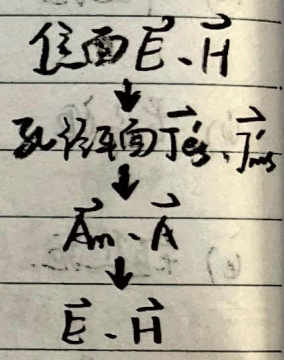
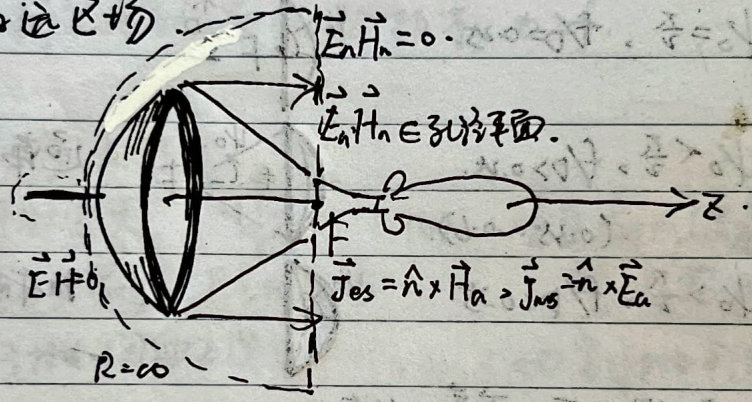
②. 顶点前安装补偿圆盘.

③. 隔量馈源法.

$$S = \frac{\lambda^2}{4\pi} G_{\text{馈源}} \quad (\text{馈源增益}) \quad d = \sqrt{\frac{4F\lambda}{\pi}}, \quad l = (2n+1)\frac{\lambda}{4} - \frac{\lambda}{4} \quad \psi_1 = a_1 (VF)^2 + a_2 (VF) - a_3 \text{ (rad)}$$

8. 求抛物面天线的远区场

I. 等效法.



a. 求位置上的 \vec{E}_n, \vec{H}_n : 由波方程及透射和反射特性.

b. 等效平面上 \vec{E}_n, \vec{H}_n , 其中 $\vec{E}_n = 0$

c. 电场源等效原理 + 镜像定理. 求 \vec{J}_{s0}, \vec{J}_s

d. 由 \vec{J}_s 求 \vec{A}_m, \vec{A} , \vec{J}_{s0} 求 \vec{A} .

e. 由 \vec{A}_m 或 \vec{A} 算 \vec{E} 和 \vec{H} .

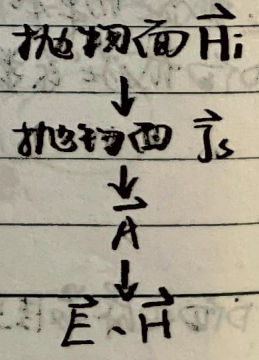
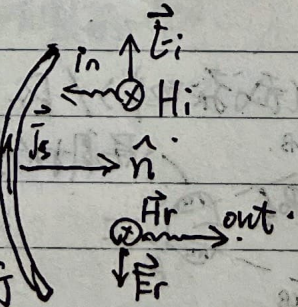
II. 等效面电流法:

a. $\vec{J}_s = (\hat{n} \times \vec{H}_i) + (\hat{n} \times \vec{H}_r)$
 $= 2(\hat{n} \times \vec{H}_i)$. 如同H相等

b. 由波方程求解 $\vec{H}_i \in S_i$

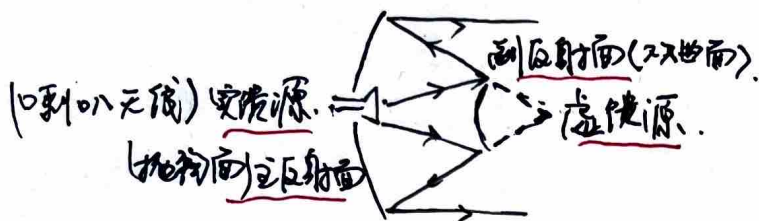
c. 由 \vec{J}_s 求 \vec{A} , 积分在四面进行

d. 由 \vec{A} 求 \vec{E}, \vec{H} .



§15 卡塞格伦天线

① 结构及工作原理

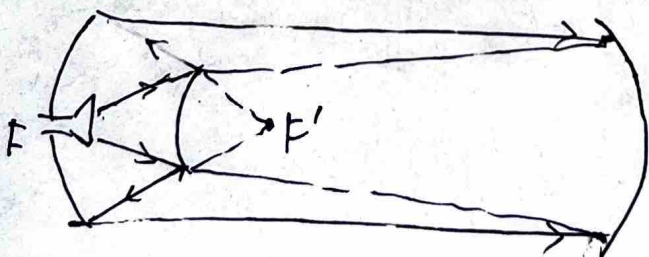


② 优点:

- 1) 口面上场分布容易调到最佳, 有内反射面可调节.
- 2) 结构紧凑, 馈电方便 — 后馈
- 3) 阻抗匹配良好 — 双曲面为扩散反射.
- 4) "具有长焦距抛物面的电性能" 和 "机械性能" 皆好.

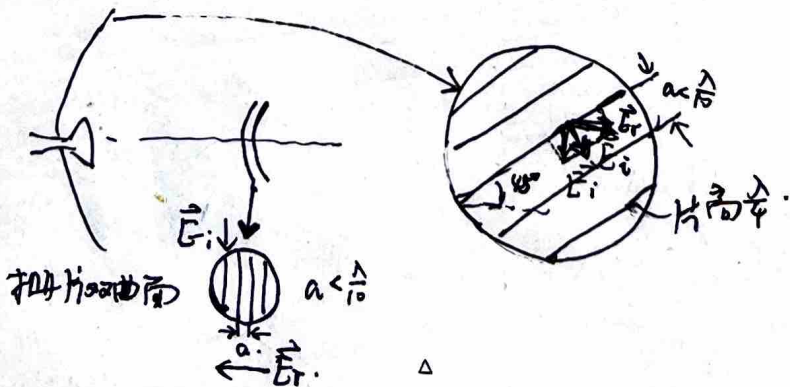
③ 两种分析方法:

- a. 虚馈源法 (等效馈源法).
- b. 等效抛物面法.



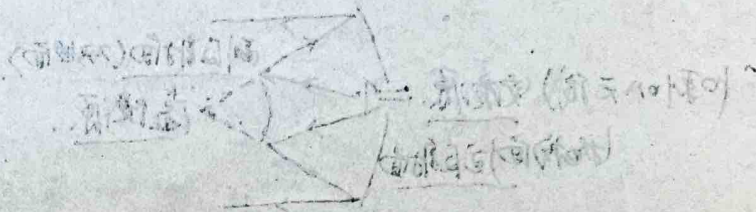
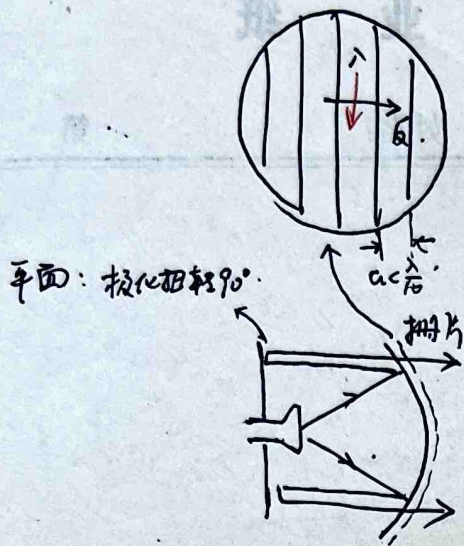
等效抛物面, 虚馈源, 双曲面, 抛物面
定后, 等效抛物面法

④ 副反射面的遮挡可用 "极化面扭转 90° " 来解决.



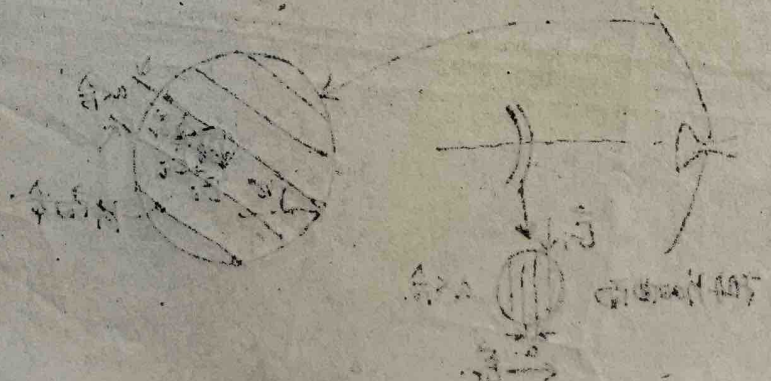
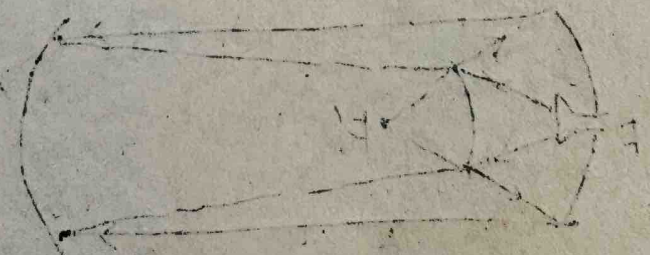
反射出去无遮挡

⑤ 李用卡塞格伦天镜.



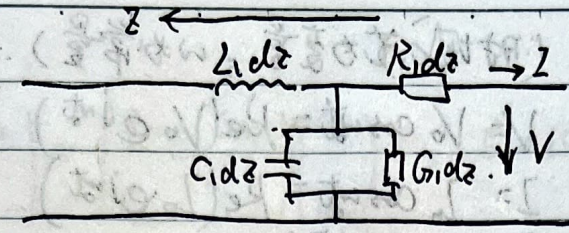
卷 6.22 周二 下午 2:30-4:30
 建馆报告厅

各疑: 伟 1003# 62773748. 6月21日



初步复习

传输线:



无耗时: $R_1 = G_1 = 0$

- 频域:
- 电容 $V(j\omega) = \frac{1}{j\omega C} I(j\omega)$
 - 电感 $V(j\omega) = j\omega L I(j\omega)$
 - 电阻 $V(j\omega) = R I(j\omega)$

频域中列写传输线方程:

$$dV(j\omega, z) = I(j\omega, z) j\omega L_1 dz$$

$$dI(j\omega, z) = V(j\omega, z) j\omega C_1 dz$$

解得

$$V(j\omega, z) = V_+(j\omega) e^{j\omega \sqrt{L_1 C_1} z} + V_-(j\omega) e^{-j\omega \sqrt{L_1 C_1} z} \quad (1)$$

$$I(j\omega, z) = I_+(j\omega) e^{j\omega \sqrt{L_1 C_1} z} + I_-(j\omega) e^{-j\omega \sqrt{L_1 C_1} z} \quad (2)$$

$$= \frac{1}{\sqrt{L_1/C_1}} [V_+(j\omega) e^{j\omega \sqrt{L_1 C_1} z} - V_-(j\omega) e^{-j\omega \sqrt{L_1 C_1} z}]$$

$$Z_c \triangleq \frac{1}{\sqrt{L_1 C_1}}, \quad \text{特 } \triangleq V_+ / j\omega$$

$$V_+(j\omega, z) \triangleq V_+(j\omega) e^{j\omega \sqrt{L_1 C_1} z}, \quad V_-(j\omega, z) \triangleq V_-(j\omega) e^{-j\omega \sqrt{L_1 C_1} z}$$

$$I_+(j\omega, z) \triangleq V_+(j\omega, z) / Z_c, \quad I_-(j\omega, z) \triangleq -V_-(j\omega, z) / Z_c$$

$$\text{则 } V(j\omega, z) = V_+(j\omega, z) + V_-(j\omega, z) \quad (3)$$

$$I(j\omega, z) = I_+(j\omega, z) + I_-(j\omega, z) \quad (4)$$

$$= V_+(j\omega, z) / Z_c - V_-(j\omega, z) / Z_c$$

$$\text{将 (3) (4) 代入 (1), 得 } V(t, z) = V_+(t + \sqrt{L_1 C_1} z) + V_-(t - \sqrt{L_1 C_1} z) \quad (5)$$

$$I(t, z) = I_+(t + \sqrt{L_1 C_1} z) + I_-(t - \sqrt{L_1 C_1} z) \quad (6)$$

边界条件

$$\begin{cases} V(j\omega, 0) = V_+(j\omega) + V_-(j\omega) = I(j\omega, 0) Z_c(j\omega) \\ I(j\omega, 0) = \frac{1}{Z_c} [V_+(j\omega) - V_-(j\omega)] \end{cases}$$

$$\begin{cases} V(j\omega, l) = V_+(j\omega) e^{j\omega \sqrt{L_1 C_1} l} + V_-(j\omega) e^{-j\omega \sqrt{L_1 C_1} l} = V_g(j\omega) - I(j\omega, l) Z_g(j\omega) \\ I(j\omega, l) = \frac{1}{Z_c} (V_+(j\omega) e^{j\omega \sqrt{L_1 C_1} l} - V_-(j\omega) e^{-j\omega \sqrt{L_1 C_1} l}) \end{cases} \quad (7)$$

$$\text{将 (7) 代入 (5), (6), 得 } [V_+(j\omega) + V_-(j\omega)] / Z_c(j\omega) = [V_+(j\omega) - V_-(j\omega)] / Z_c \quad (8)$$

$$(V_+(j\omega) + V_-(j\omega)) / Z_c(j\omega) = V_g(j\omega) / Z_g(j\omega) - [V_+(j\omega) - V_-(j\omega)] / Z_c$$

可解出 $V_+(j\omega)$ 和 $V_-(j\omega)$

二. 时域场下的运算规律: (时域: v 为变量; ω 为常量).

时谐场: $V = V_0 \cos \omega t = \text{Re}(V_0 e^{j\omega t})$, $\tilde{V} \triangleq V_0 e^{j\omega t}$
 $I = I_0 \cos \omega t = \text{Re}(I_0 e^{j\omega t})$, $\tilde{I} \triangleq I_0 e^{j\omega t}$

电容: ~~$I(t) = C \frac{dV(t)}{dt}$~~
 $I(t) = C \frac{dV(t)}{dt} = j\omega C \text{Re}(V_0 e^{j\omega t})$
 $= C \text{Re}(j\omega V_0 e^{j\omega t})$
 $= \text{Re}(j\omega C \cdot V_0 e^{j\omega t})$

电感: $\tilde{I}(t) = j\omega C V_0 e^{j\omega t} = j\omega C \cdot \tilde{V}$ ①

$V(t) = L \frac{dI(t)}{dt} = \text{Re}(j\omega L I_0 e^{j\omega t})$
 $\tilde{V}(t) = j\omega L \cdot \tilde{I}$ ②

电阻: $V(t) = R I(t)$
 $\tilde{V}(t) = R \tilde{I}(t)$ ③

$\because e^{j\omega t}$ 因子对线性运算的不变性, $\therefore \tilde{V}(\vec{r}, t), \tilde{I}(\vec{r}, t)$ 可直接写成 $\tilde{V}(\vec{r}), \tilde{I}(\vec{r})$
 \therefore ①②③式, \therefore 可得电容电感电阻等阻集列方程。
 上述规律是“路”的规律, “场”的规律类似, 将 $E(\vec{r}, t), H(\vec{r}, t)$ 直接写成 $\tilde{E}(\vec{r}), \tilde{H}(\vec{r})$

三. 微波网络的研究方法.

为了定义任意截面沿 z 方向单模传输的均匀波导参考面上的模式电压和模式电流, 作如下规定: 只考虑沿一个方向的传播 \hat{z} 或 $-\hat{z}$.

- (1) $V(z) \triangleq E_T$, $I(z) \triangleq H_T$
- (2) $\tilde{P} = V(z) \cdot \tilde{I}^*(z)$
- (3) $Z_c = V(z) / \tilde{I}(z)$

进入网络: 内向波 $a = V_+ / \sqrt{Z_c}$ 向网络端; $a' = a e^{j\theta}$, $b' = b e^{j\theta}$
 离开网络: 外向波 $b = V_- / \sqrt{Z_c}$ 向网络端; $b' = b e^{j\theta}$; $a' = a e^{j\theta}$

时N端口网络, 定义

$$\begin{pmatrix} b_1 \\ \vdots \\ b_n \end{pmatrix} = \begin{pmatrix} S_{11} & S_{1n} \\ \vdots & \vdots \\ S_{n1} & S_{nn} \end{pmatrix} \begin{pmatrix} a_1 \\ \vdots \\ a_n \end{pmatrix}, \quad \vec{b} = [S] \vec{a} \quad \left\{ \begin{array}{l} i \text{口匹配: } S_{ii} = 0 \\ i \text{口接匹配负载: } \Gamma_i' = 0 \end{array} \right.$$

(1) 互易: $S_{ij} = S_{ji}, [S] = [S]^T$

(2) 无耗: $[S]^H [S] = I$

时二端口网络

(1) 互易: $S_{12} = S_{21}$

(2) 对称: $|S_{12}| = |S_{21}|, |S_{11}| = |S_{22}|, |S_{11}|^2 + |S_{21}|^2 = 1, |S_{12}|^2 + |S_{22}|^2 = 1$

1) 端口1匹配则端口2匹配, 电压传输系数幅值为1.

$$|S_{11}| = |S_{22}| = 0, |S_{12}| = |S_{21}| = 1$$

2) 不能实现单向隔离, 隔离是双向的

$$|S_{12}| = |S_{21}| = 0$$

3) 双向隔离时, 产生全反射

$$|S_{12}| = |S_{21}| = 0, |S_{11}| = |S_{22}| = 1$$

(3) 对称: $S_{11} = S_{22}, S_{12} = S_{21}$

1) 本征方程 $\begin{bmatrix} S_{11} - S_j & S_{12} \\ S_{12} & S_{11} - S_j \end{bmatrix} \begin{bmatrix} u_1^j \\ u_2^j \end{bmatrix} = 0$

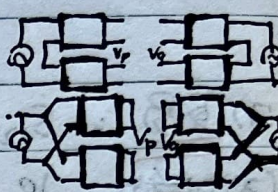
2) 本征值 $\begin{cases} S_1 = S_{11} + S_{12} \\ S_2 = S_{11} - S_{12} \end{cases} \Rightarrow \begin{cases} S_{11} = \frac{S_1 + S_2}{2} \\ S_{12} = \frac{S_1 - S_2}{2} \end{cases}$

本征矢: $S_1 \Rightarrow u_1 = \frac{1}{\sqrt{2}} (1, 1)^T$
 $S_2 \Rightarrow u_2 = \frac{1}{\sqrt{2}} (1, -1)^T$

意义: 以 u_1 作为两个端口的入射波 a , 则 $b = [S] u_1 = S_1 u_1$, 反射系数为 S_1 .
 以 u_2 作为两个端口的入射波 a , 则 $b = [S] u_2 = S_2 u_2$, 反射系数为 S_2 .
 用 u_1 的两个分量对两个端口来说等幅同向, 对应于中间开路情况
 用 u_2 的两个分量对两个端口来说等幅反向, 对应于中间短路情况

(4) 指标

- 1) 电压传输系数 $T_V = S_{21}$
- 2) 功率传输系数 $T_P = |S_{21}|^2$
- 3) 插入衰减 $L = \frac{1}{|S_{11}|^2}$
- 4) 插入相移 $\phi_{in} = \arg S_{21}$
- 5) 群时延 $t_d = \frac{d}{d\omega} \phi_{in}$
- 6) 输入驻波比 $\rho = \frac{1+|S_{11}|}{1-|S_{11}|}$

- (5) 阻抗矩阵: 串联: $[Z] = \sum [Z_i]$ $V_p = V_q = 0$: 有效串联
- 导纳矩阵: 并联: $[Y] = \sum [Y_i]$ $V_p = V_q = 0$: 有效并联
- 级联矩阵: 级联: $[A] = \prod [A_i]$ (用 $V_1, Z_1, V_2, -I_2$ 表示)
- 传输矩阵: 级联: $[T] = \prod [T_i]$ (用 a_1, b_1, a_2, b_2 表示)
- 串并矩阵: 串并联: $[H] = \sum [H_i]$
- 并串矩阵: 并串联: $[G] = \sum [G_i]$
- 

四. 波导到传输线 (时谐、均匀、无源、无耗)

1. 纵横关系 (例子: $\vec{V} = \vec{V}_T + \vec{V}_z$; $\vec{V} = \dots = \vec{V}_1 + \vec{V}_2$)

知原、时谐时:

沿 \hat{z} 传 (波矢 $\hat{z} = k_z$)

沿 \hat{z} 传 (波矢 $\hat{z} = k_z$)

$$(k^2 - k_z^2) \vec{H}_T = -j\omega \epsilon_0 \hat{z} \times \nabla_T E_z - jk_z \nabla_T H_z$$

$$(k^2 - k_z^2) \vec{E}_T = j\omega \mu_0 \hat{z} \times \nabla_T H_z - jk_z \nabla_T E_z$$

$$(k^2 - k_z^2) \vec{H}_T = j\omega \epsilon_0 \hat{z} \times \nabla_T E_z + jk_z \nabla_T H_z$$

$$(k^2 - k_z^2) \vec{E}_T = -j\omega \mu_0 \hat{z} \times \nabla_T H_z + jk_z \nabla_T E_z$$

2. TE 波: $E_z = 0$

沿 \hat{z} 传:

沿 \hat{z} 传

$$\vec{H}_T = -\frac{jk_z}{k^2 - k_z^2} \nabla_T H_z$$

$$\vec{E}_T = \frac{j\omega \mu_0}{k^2 - k_z^2} \hat{z} \times \nabla_T H_z$$

$$\vec{E}_T = -\frac{\omega \mu_0}{k_z} \hat{z} \times \vec{H}_T = -\eta_{TE} \hat{z} \times \vec{H}_T$$

$$\vec{E}_T = \eta_{TE} \hat{z} \times \vec{H}_T$$

边界条件: $\frac{\partial H_z}{\partial n} |_{\text{边界}} = 0$

算子: $\nabla = \nabla_T + \nabla_z$, $\nabla^2 = \dots = \nabla_T^2 + \nabla_z^2$. T : 横, z : 纵

~~$\nabla^2 H_z + k^2 H_z = 0$~~

沿 z 轴:

~~$H_z = H_z(\pi) \cdot e^{jk_z z}$~~

沿 T 轴:

~~$H_z = H_z(\pi) \cdot e^{jk_z z}$~~

都得到

~~$\nabla_T^2 H_z(\pi) + (k^2 - k_z^2) H_z(\pi) = 0$~~

1. TE波: $E_z = 0$

$\begin{cases} \nabla^2 H_z + k^2 H_z = 0 \rightarrow \nabla_T^2 H_z(\pi) + (k^2 - k_z^2) H_z(\pi) = 0, H_z(z) = e^{-jk_z z} \text{ or } e^{jk_z z} \\ \frac{\partial H_z}{\partial n} \Big|_{\text{边界}} = 0 \end{cases}$

解得沿 z 轴和一 z 轴的 H_z ; k_z . 定义 $\eta_{TE}(\omega) = \frac{\omega \mu}{k_z}$

2. TM波: $H_z = 0$

$\begin{cases} \nabla^2 E_z + k^2 E_z = 0 \rightarrow \nabla_T^2 E_z(\pi) + (k^2 - k_z^2) E_z(\pi) = 0, E_z(z) = e^{-jk_z z} \text{ or } e^{jk_z z} \\ E_z \Big|_{\text{边界}} = 0 \end{cases}$

解得沿 z 轴和一 z 轴的 E_z ; k_z . 定义 $\eta_{TM}(\omega) = \frac{k_z}{\omega \epsilon}$

3. TEM波: $E_z = 0, H_z = 0$, $\vec{W}_T \triangleq \vec{E}_T \text{ or } \vec{H}_T$

$\begin{cases} \nabla^2 \vec{W}_T + k^2 \vec{W}_T = 0 \rightarrow \nabla_T^2 \vec{W}_T(\pi) = 0 \rightarrow \nabla_T \cdot \vec{W}_T = \nabla_T \times \vec{W}_T = 0, W_T(z) = e^{-jk_z z} \text{ or } e^{jk_z z} \\ \text{无 } (\nabla \cdot \text{const} = v) \end{cases}$ 根据空心金属波导中不存在 TEM 波.

解得沿 z 轴和一 z 轴的 E_x, E_y, H_x, H_y . 定义 $\eta_{TEM} = \sqrt{\frac{\mu}{\epsilon}}, k_z = k$.

4. 由无源、时谐和 $H(z), E(z) = e^{-jk_z z} \text{ or } e^{jk_z z}$, 得纵横关系式 ~~($\nabla^2 H_z + k^2 H_z = 0$)~~

沿 z 轴: $\begin{cases} (k^2 - k_z^2) \vec{H}_T = -j\omega \epsilon \hat{z} \times \nabla_T E_z - jk_z \nabla_T H_z \\ (k^2 - k_z^2) \vec{E}_T = j\omega \mu \hat{z} \times \nabla_T H_z - jk_z \nabla_T E_z \end{cases}$

沿 T 轴: $\begin{cases} (k^2 - k_z^2) \vec{H}_T = j\omega \epsilon \hat{z} \times \nabla_T E_z + jk_z \nabla_T H_z \\ (k^2 - k_z^2) \vec{E}_T = -j\omega \mu \hat{z} \times \nabla_T H_z + jk_z \nabla_T E_z \end{cases}$

由此解出 TE 和 TM 波的 \vec{H}_T, \vec{E}_T , (根据 H_z, E_z).

5. 参数:

(1) 导波波数: $k_z \geq 0$. ($v_p = \frac{\omega}{k_z}, v_g = \frac{d\omega}{dk_z}$); 导波波长: $\lambda_g = \frac{2\pi}{k_z}$; 导波频率: 自变量.

(2) 截止波数: $k_c \triangleq \sqrt{k^2 - k_z^2}$; 截止波长: $\lambda_c = \frac{2\pi}{k_c}$; 截止频率: $f_c = \frac{k_c \cdot c}{2\pi}$.

(1) 是导波的实际参数, 有物理意义 (2) 中参数与波导尺寸有关, 用于区与尺寸.

正向: e^{jkz} 反向: e^{-jkz} $\Rightarrow \nabla \cdot \nabla + \nabla = \nabla$

波腹: $\phi - 2kz = 2k\pi$, 波节: $\phi - 2kz = \pi + 2k\pi$

6. 传输线描述的推导.

波动方程

根据 1, 2, 3, 各模式具有正交性, 对于每一模式, 由分离变量的结果:

$$\begin{cases} \frac{\partial^2}{\partial z^2} \vec{E}_T + k_z^2 \vec{E}_T = 0 \\ \frac{\partial^2}{\partial z^2} \vec{H}_T + k_z^2 \vec{H}_T = 0 \end{cases} \Rightarrow \begin{cases} \vec{E}_T(z) = \vec{E}_T^+ e^{jk_z z} + \vec{E}_T^- e^{-jk_z z} \\ \vec{H}_T(z) = \vec{H}_T^+ e^{jk_z z} + \vec{H}_T^- e^{-jk_z z} \end{cases}$$

$$\begin{cases} \vec{E}_T \triangleq V \hat{e}(x, y) \\ \vec{H}_T \triangleq I \hat{h}(x, y) \end{cases} \Rightarrow \begin{cases} \vec{E}_T^+ \triangleq V_+ \hat{e}(x, y) \\ \vec{H}_T^+ \triangleq I_+ \hat{h}(x, y) \end{cases} \quad \begin{cases} V = \int \vec{E} \cdot d\vec{l} \\ I = \oint \vec{H} \cdot d\vec{l} \end{cases}$$

$$\begin{cases} \frac{\partial^2}{\partial z^2} V + k_z^2 V = 0 \\ \frac{\partial^2}{\partial z^2} I + k_z^2 I = 0 \end{cases}$$

求解

$$\begin{cases} V = V_+ + V_- = V_+ e^{jk_z z} + V_- e^{-jk_z z} \\ I = I_+ + I_- = I_+ e^{jk_z z} + I_- e^{-jk_z z} \end{cases} \quad \text{①} \quad \text{②}$$

为可证

$$V_+ / I_+ = -V_- / I_-$$

(1) $Z_c \triangleq V_+ / I_+ = -V_- / I_-$, $Y_c = 1 / Z_c$. eg. 同轴线的 $Z_c = 60 \sqrt{\epsilon_r} \ln \frac{D}{d}$

(2) $\Gamma \triangleq V / V_+ = -I / I_+ = \frac{V_0 e^{-jk_z z}}{V_+ e^{jk_z z}} = \Gamma e^{-j2k_z z} = |\Gamma| e^{j(\phi_F - 2k_z z)}$ ③

$$\Gamma = \frac{Z_L - Z_c}{Z_L + Z_c} = \frac{R_F + jX_F - Z_c}{R_F + jX_F + Z_c}$$

$$|\Gamma| = \sqrt{\frac{(R_F - Z_c)^2 + X_F^2}{(R_F + Z_c)^2 + X_F^2}}$$

∵ 无源负载 $R_F \geq 0$

$$\therefore |\Gamma| \leq 1$$

$$\therefore |\Gamma| \leq 1$$

(3) $\bar{z}_i \triangleq \frac{V}{I} / Z_c = \frac{V_+ + V_-}{I_+ + I_-} / Z_c = \frac{V_+(1 + \Gamma)}{I_+(1 - \Gamma)} / Z_c = \frac{1 + \Gamma}{1 - \Gamma} = \frac{Z_L + j \tan \theta Z_c}{1 + j Z_L \tan \theta / Z_c}$ ④

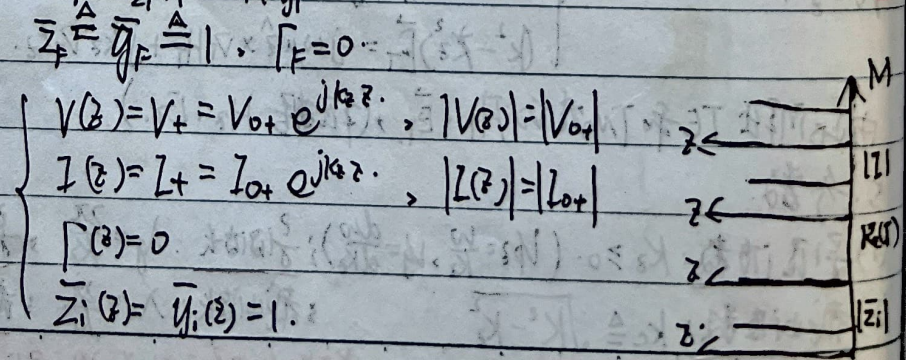
(4) $\bar{y}_i \triangleq \frac{I}{V} / Y_c = \frac{I_+ + I_-}{V_+ + V_-} / Y_c = \frac{1 - \Gamma}{1 + \Gamma} = \frac{Y_L + j \tan \theta Y_c}{1 + j Y_L \tan \theta / Y_c}$ ⑤

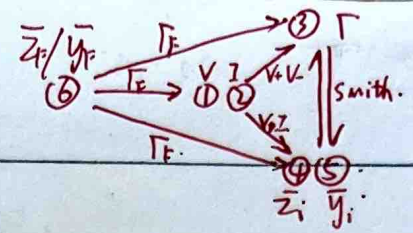
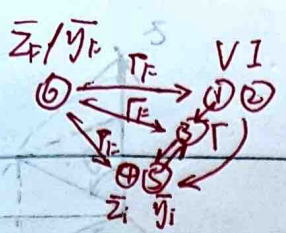
(5) $\Gamma = \frac{\bar{z}_i - 1}{\bar{z}_i + 1} = \frac{1 - \bar{y}_i}{1 + \bar{y}_i}$ ⑥

(5) $\rho = \frac{V_{max}}{V_{min}} = \frac{1 + |\Gamma|}{1 - |\Gamma|} e^{j(\phi)}$

(6) $\rho_{min} \triangleq \frac{\phi - \pi}{2kz}$

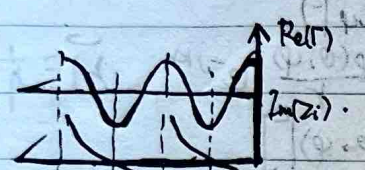
① 行波状态:



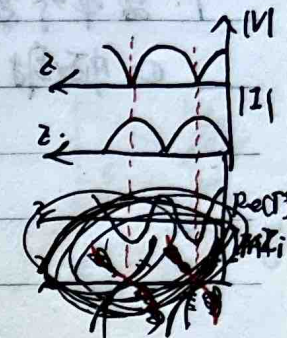


② 驻波状态

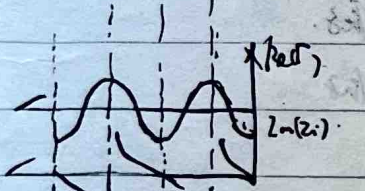
1) 终端开路 $Z_F \triangleq \infty / Y_F \triangleq 0, \Gamma_F = +1$



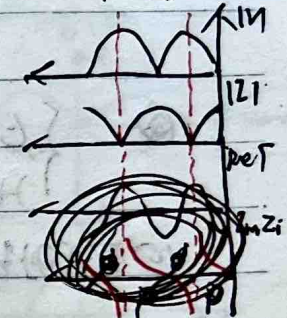
$$\begin{cases} V(z) = 2V_0+ \cos kz \\ I(z) = 2j \frac{V_0+}{Z_c} \sin kz \\ \Gamma(z) = +e^{-j2kz} \\ Z_i(z) = -j \cot kz, \bar{Y}_i(z) = j \tan kz \end{cases}$$



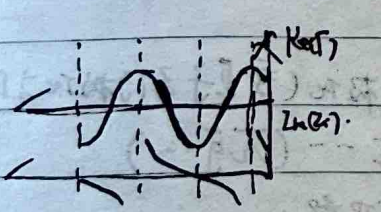
2) 终端短路 $Z_F \triangleq 0 / Y_F \triangleq \infty, \Gamma_F = -1$



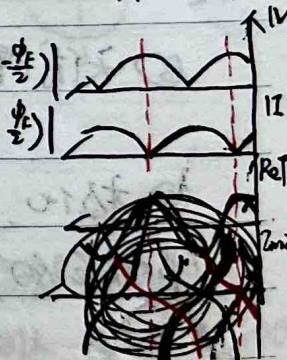
$$\begin{cases} V(z) = j2V_0+ \sin kz \\ I(z) = \frac{2V_0+}{Z_c} \cos kz \\ \Gamma(z) = -e^{-j2kz} \\ Z_i(z) = j \tan kz, \bar{Y}_i(z) = -j \cot kz \end{cases}$$



3) 终端纯电抗 $Z_F \triangleq jx / Y_F \triangleq jb, |\Gamma_F| = 1 (\Gamma_F = e^{j\phi})$

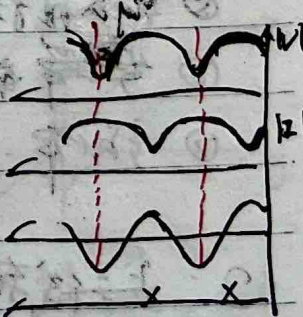


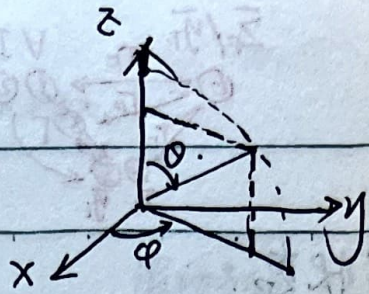
$$\begin{cases} V(z) = 2V_0+ e^{j\frac{\phi}{2}} \cos(kz - \frac{\phi}{2}) \\ I(z) = 2j \frac{V_0+}{Z_c} e^{j\frac{\phi}{2}} \sin(kz - \frac{\phi}{2}) \\ \Gamma(z) = e^{j(\phi - 2kz)} \\ Z_i(z) = -j \cot(kz - \frac{\phi}{2}), \bar{Y}_i(z) = j \tan(kz - \frac{\phi}{2}) \end{cases}$$



③ 驻波状态

$$\begin{cases} V(z) = V_0+ (1 + \Gamma_F e^{-j2kz}) \\ I(z) = \frac{V_0+}{Z_c} (1 - \Gamma_F e^{-j2kz}) \\ \Gamma(z) = |\Gamma_F| e^{j(\phi - 2kz)} \\ Z_i(z) = \frac{1 + \Gamma_F e^{-j2kz}}{1 - \Gamma_F e^{-j2kz}}, \bar{Y}_i(z) = \frac{1 - \Gamma_F e^{-j2kz}}{1 + \Gamma_F e^{-j2kz}} \end{cases}$$





五. 天线

1. 基本参数:

① 辐射方向图, 远区场中只有 E 和 H , 球面波:

$$\vec{S} = \frac{1}{2} (\vec{E} \times \vec{H}^*) = \hat{r} \frac{1}{2\eta} (|E_\theta|^2 + |E_\phi|^2)$$

$$E_\theta = \frac{f_\theta(\theta, \phi)}{r} e^{-jkr}, \quad E_\phi = \frac{f_\phi(\theta, \phi)}{r} e^{-jkr}, \quad \vec{H} = \hat{r} \times \vec{E}$$

$$\therefore \vec{S} = \frac{1}{2\eta r^2} (|f_\theta(\theta, \phi)|^2 + |f_\phi(\theta, \phi)|^2)$$

$$F(\theta, \phi) \triangleq r^2 S = \frac{1}{2\eta} (|f_\theta(\theta, \phi)|^2 + |f_\phi(\theta, \phi)|^2)$$

$$F_n(\theta, \phi) \triangleq F(\theta, \phi) / F_{max}(\theta, \phi)$$

② 辐射方向图: \vec{E} 所在平面, e.g. $\phi = \text{const}$ for 振子.
 H面方向图, \vec{H} 所在平面, e.g. $\theta = 90^\circ$ for 振子

③ 方向性系数 (辐射功率相同)

$$D(\theta, \phi) \triangleq \frac{S_r(\theta, \phi)}{P_r / 4\pi r^2}$$

④ 天线增益 (输入功率相同)

$$G(\theta, \phi) \triangleq \frac{S_r(\theta, \phi)}{P_{in} / 4\pi r^2}$$

⑤ 极化: 线极化: 平行极化 (平行于辐射面), 垂直极化 (垂直于平行极化方向).

(圆极化方向) 圆极化: 右旋圆极化 (右手螺旋法则), 左旋 (左手...)

椭圆极化: = 逆时针和顺时针不等幅圆极化波叠加.

⑥ 输入阻抗 Z_{in} = 端点电压 / 端点电流. (横电面上)

⑦ ~~辐射~~ 辐射电阻 $R_{rad} = 2P_r / I^2$.

⑧ 频带: 满足反射系数, 增益等要求的频率范围.

2. 天线辐射场

电流源

$$\vec{A}_e(\vec{r}) = \frac{\mu}{4\pi} \int \frac{e^{jk|\vec{r}-\vec{r}'|}}{|\vec{r}-\vec{r}'|} \vec{J}(\vec{r}') dV', \quad \text{磁流源: } \vec{A}_m(\vec{r}) = \frac{\epsilon}{4\pi} \int \frac{e^{jk|\vec{r}-\vec{r}'|}}{|\vec{r}-\vec{r}'|} \vec{J}_m(\vec{r}') dV'$$

$$\vec{H}_e = \nabla \times \vec{A}_e$$

$$\vec{H}_m = -j\omega \vec{A}_m - \frac{1}{\omega\epsilon\mu} \nabla(\nabla \cdot \vec{A}_m)$$

$$\vec{E}_e = -j\omega \vec{A}_e - \frac{1}{\omega\epsilon\mu} \nabla(\nabla \cdot \vec{A}_e)$$

$$\vec{E}_m = -\frac{1}{\epsilon} \nabla \times \vec{A}_m$$

3. 点天线 ($Z = Z_0 e^{j\omega t}$)

近区: \vec{S} 纯虚数, 储能场, 无辐射.

远区: \vec{S} 实数, 辐射场, 球面波.

$$H\phi \approx \frac{Z_0 I}{4\pi r} e^{-jkr} \frac{j k}{r} \sin\theta \Rightarrow E_0 / \eta$$

$$E_0 \approx \frac{Z_0 I}{4\pi r} e^{-jkr} j k r \sin\theta$$

$$S_r = \frac{1}{2} (E_0 \times H\phi^*) \cdot \hat{r} = \frac{\eta}{8} \left(\frac{Z_0 I}{r}\right)^2 \frac{\sin^2\theta}{r^2}$$

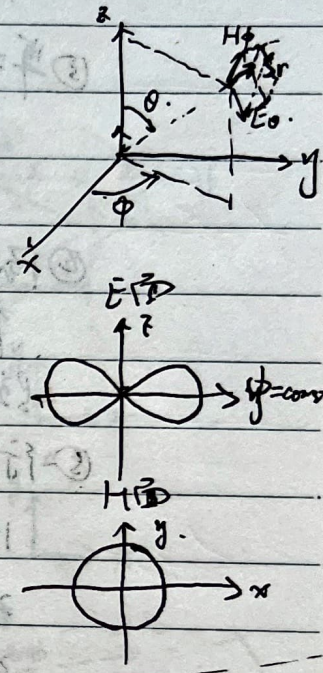
$$P_r = \oint S_r \cdot d\vec{s} = 4\pi r^2 \left(\frac{Z_0 I}{r}\right)^2 \frac{\eta}{8}$$

$$R_r = 2P_r / Z_0^2 = 80\pi^2 \left(\frac{l}{\lambda}\right)^2$$

$$f_n(\theta) = \sin\theta, \quad f_n(\theta) = \sin\theta$$

$$f_n(\theta) \triangleq \frac{1}{\sqrt{2}} \Rightarrow |\theta_2 - \theta_1| = 90^\circ \text{ 半功率角.}$$

$$D(\theta, \phi) = \frac{S_r}{P_r / 4\pi r^2} = \frac{1}{2} \sin^2\theta \quad \theta = \frac{\pi}{2} \quad 1.5 = 1.76 \text{ dB.}$$



4. 线天线

远区: $dH\phi = j \frac{I dl}{4\pi r} e^{-jkr} \frac{j k}{r} \sin\theta = dl E_0 / \eta$

$$dE_0 = \frac{I dl}{4\pi r} e^{-jkr} j k r \sin\theta$$

① 对称振子: $\begin{cases} Z(z) = Z_0 \sin k(\frac{l}{2} - z') & 0 \leq z' \leq \frac{l}{2} \\ Z(z') = Z_0 \sin k(\frac{l}{2} + z') & -\frac{l}{2} \leq z' \leq 0 \end{cases} \begin{cases} \text{振幅} R \approx r \\ \text{相位} R = r - z' \cos\theta \end{cases}$

$$H\phi = j \frac{Z_0 e^{jkr}}{2\pi r} \frac{\cos(\frac{kl}{2} \cos\theta) - \cos \frac{kl}{2}}{2} = E_0 / \eta$$

$$E_0 \approx j \eta \frac{Z_0 e^{jkr}}{2\pi r} \frac{\cos(\frac{kl}{2} \cos\theta) - \cos \frac{kl}{2}}{\sin\theta}$$

$$S_r \approx \eta \frac{Z_0^2}{8\pi^2 r^2} \left[\frac{\cos(\frac{kl}{2} \cos\theta) - \cos \frac{kl}{2}}{\sin\theta} \right]^2$$

$$l = \frac{\lambda}{2}: P_r = 36.54 Z_0^2$$

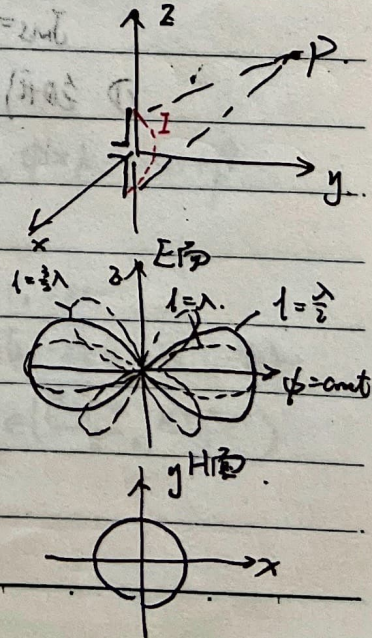
$$\Downarrow R_r = 73 \Omega = Z_{in}$$

$$f_n(\theta) = \frac{\cos(\frac{\pi}{2} \cos\theta)}{\sin\theta}, \quad f_n(\theta) = \frac{f_n(\theta)}{(1 - \cos \frac{kl}{2})^2}$$

$$f_n(\theta) \triangleq \frac{1}{\sqrt{2}} \Rightarrow |\theta_2 - \theta_1| = 78^\circ \text{ 半功率角.}$$

$$D(\theta, \phi) \stackrel{\theta=0}{=} 1.64 = 2.15 \text{ dB}$$

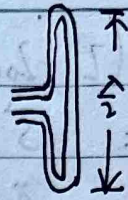
$$l = \lambda: R_r = 200 \Omega; \quad l = \frac{3}{2} \lambda: R_r = 106 \Omega$$



② 折叠振子

$R_r \approx 2 \times 73 \Omega$

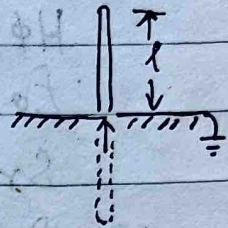
$Z_{in} \approx 4 \times 73 \Omega$



③ 单极天线

$D = 2 D_{\text{折叠振子}}$

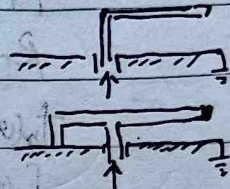
$l = \frac{\lambda}{4}$ 时, $D = 2 \times 1.64 = 3.4 = 5.16 \text{ dB}$



④ 例2/例F天线: 弯折的单极天线

例F中增加的一节用来增加 R_{rad}

△ 驻波天线 — ①②③④: 终端开路



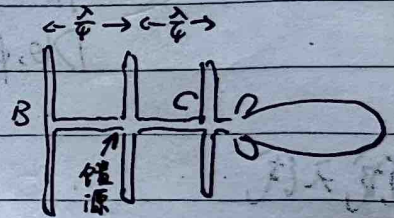
⑤ 行波天线 — 八字形

1号稍短于 $\lambda/2$: Z_{inB} 感性

2号等于 $\lambda/2$: 在1、3号感应出场 (远场)

3号稍短于 $\lambda/2$: Z_{inC} 容性

∴ 1号、2号或3号, 均在 y 同相叠加, 在 x 反相叠加



5. 面天线

远区: 电导体/磁导体 等效 + 镜像原理

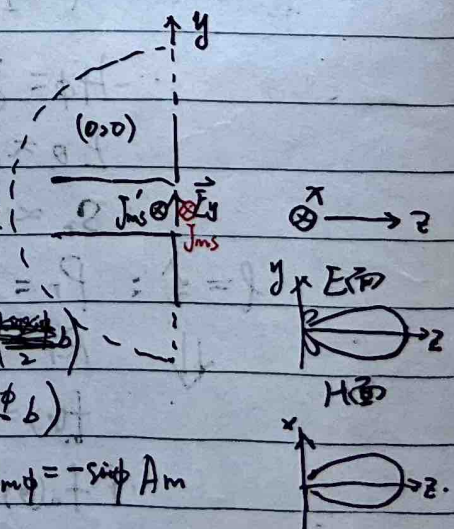
$\vec{J}_{ms} = -\hat{n} \times \vec{E} / \vec{J}_e = \hat{n} \times \vec{H}$

① 均匀波导口. ($\vec{E}_y = \hat{y} E_0$)

$\vec{J}_{ms} = \hat{x} \vec{J}_m = \hat{x} \cdot 2 E_0$

幅: $R \approx r$

相: $R \approx r - r \cos \phi$



$H_{m0} = \int_{-b/2}^{b/2} \int_{-a/2}^{a/2} \frac{\epsilon_0 ab e^{-jkr}}{2r} \cos \phi \cos \theta \frac{e^{-jkr}}{2} \frac{a}{2} \frac{b}{2}$

$\vec{A}_m = \hat{x} \cdot \frac{\epsilon_0 e^{-jkr}}{2r} E_0 \cdot ab \text{Sa} \left(\frac{ksx \cos \theta}{2} a \right) \text{Sa} \left(\frac{kry \cos \theta}{2} b \right)$

$A_{mr} = \sin \theta \cos \phi A_m, A_{m\phi} = \cos \theta \cos \phi A_m, A_{m\theta} = -\sin \phi A_m$

$H_{m0} \approx -j\omega A_{m0}, H_{m\phi} \approx -j\omega A_{m\phi}$

$E_{m0} \approx \eta H_{m\phi}, E_{m\phi} \approx -\eta H_{m0}$

$\phi = 90^\circ: f_{n, E} = S_a \left(\frac{k b}{2} \sin \theta \right) \triangleq \frac{1}{\sqrt{2}}, \quad 2\theta_{0.5, E} \approx 51^\circ \cdot \frac{\lambda}{b}$
 $\phi = 0^\circ: f_{n, H} = S_a \left(\frac{k a}{2} \sin \theta \right) \triangleq \frac{1}{\sqrt{2}}, \quad 2\theta_{0.5, H} \approx 51^\circ \cdot \frac{\lambda}{a}$

No.

Date

③ 矩形波导 ($\vec{E}_y = \hat{y} E_0 \sin \frac{\pi x}{a}$)

$2\theta_{0.5, E} = 68^\circ \cdot \frac{\lambda}{b}$

$2\theta_{0.5, H} = 68^\circ \cdot \frac{\lambda}{a}$

④ 抛物面天线

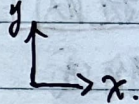
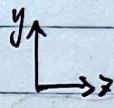
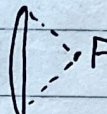
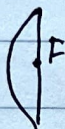
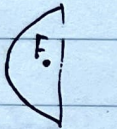
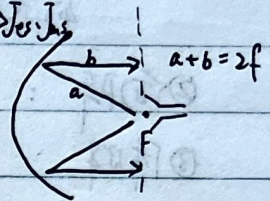
等效法: 类似于矩形波导, 抛物面上 $\vec{E} \cdot \vec{n} \Rightarrow \vec{J}_s, \vec{J}_v$

镜面电流法: 由抛物面上的 \vec{J}_s 算 \vec{A}

短焦距: 互相抵消

中焦距: 交叉极化

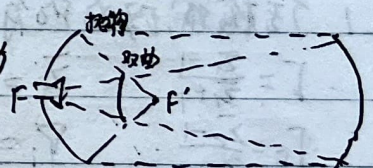
长焦距: \checkmark



④ 卡塞格伦天线: 用“极化扭转 ρ_0 ” 解决副瓣和遮挡

6. 天线阵

直接法
等效物理法: 见右图



远区: $f(\theta, \phi) = f_a(\theta, \phi) \cdot f_e(\theta, \phi) \approx f_a(\theta, \phi)$

阵列因子 单元因子

幅: $R \approx r$
相: $R \approx r \pm \frac{d}{2} \cos \theta$

① 阵列

1) 二元: $E_0 = j \frac{k \eta I_0 l}{4\pi r} \frac{e^{jkr}}{r} \sin \theta \cdot 2 \cos \frac{kd \cos \theta + \beta}{2}$
 $= j \frac{k \eta I_0 l}{4\pi r} \frac{e^{jkr}}{r} f_e(\theta, \phi) \cdot f_a(\theta, \phi)$

2) N元: $f_{an} = \sin N \frac{\phi}{2} / \sin \frac{\phi}{2}$ N 为整数, $\phi = kd \cos \theta + \beta$

$\theta_{max} = \cos^{-1} \left(\frac{\beta}{kd} \right), \quad \phi = 0$

$\theta_0 = \cos^{-1} \left(\frac{2p\pi}{Nkd} - \frac{\beta}{kd} \right), \quad \phi = \frac{2p\pi}{N}, \quad p = \pm 1, \pm 2, \dots$

$\theta_{max, \frac{1}{2}} = \cos^{-1} \left(\frac{2(p \pm \frac{1}{2})\pi}{2Nkd} - \frac{\beta}{kd} \right), \quad \phi = \frac{2(p \pm \frac{1}{2})\pi}{2N}, \quad p = (1, -2), (2, -3), (3, -4), \dots$

可见: $\theta \in (0, 180^\circ), \quad \phi \in (\beta - kd, \beta + kd), \quad \frac{\phi}{2} \in \left(\frac{\beta - kd}{2}, \frac{\beta + kd}{2} \right)$

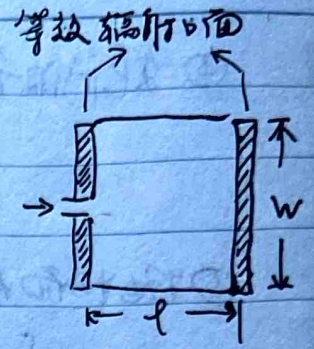
3) 宽带天线: 二元阵列

$f_{E, a} = S_a \left(\frac{k b}{2} \sin \theta \right) \cdot 2 \cos \frac{\phi}{2} \sin \theta$

$f_{H, a} = S_a \left(\frac{k a}{2} \sin \theta \right) \cdot 2 \cos \theta$

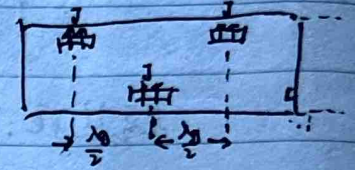
$$Z_{in} = \frac{R_r}{\rho}$$

$$R_r \approx \begin{cases} 120 \frac{\lambda}{W} & W \geq 2\lambda \\ \rho_0 \left(\frac{W}{\lambda}\right)^2 & W < 0.5\lambda \\ \left[W/120\lambda - 1/60\pi \right]^{-1} & 0.15\lambda \leq W < 2\lambda \end{cases}$$



4) 波导开缝天线: 切割同向的位移电流. 右图:

- ② 面阵: $f_a = f_{ax} \cdot f_{ay}$
- ③ 体阵: $f_a = f_{ax} \cdot f_{ay} \cdot f_{az}$



复习提纲 ⑩

一. 传输线

1. 传输线理论的有关公式.

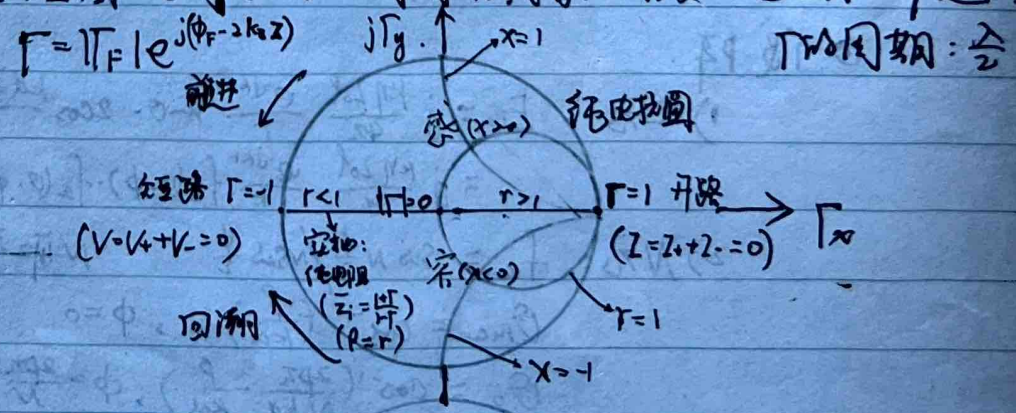
$$\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0} \quad Z_L = \frac{1 + \Gamma}{1 - \Gamma} \quad \left(= \frac{V}{I} \right) \quad Z_0 = \rho_0 \left(= \frac{V_{max}}{I_{min}} \right) \quad \Sigma = Z_{in} / Z_0$$

$$\Gamma_F = \frac{Z_F - Z_0}{Z_F + Z_0} \quad \Gamma_i = \frac{1 - \Gamma}{1 + \Gamma} \quad \left(= \frac{I}{V} \right) \quad Y_0 = \frac{1}{Z_0} \quad k = \frac{1}{\rho} \quad \bar{Y} = \frac{1}{\Sigma}$$

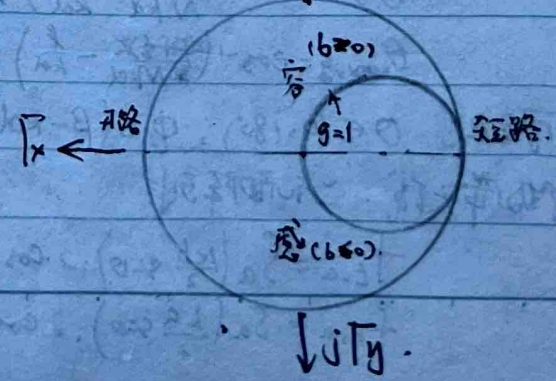
2. Smith 圆图的构造, 查图规则. 亦志圆图各线条的含义, 整体解题.

阻抗圆图:

$$\Gamma = |\Gamma_F| e^{j(\phi_F - 2\beta z)}$$

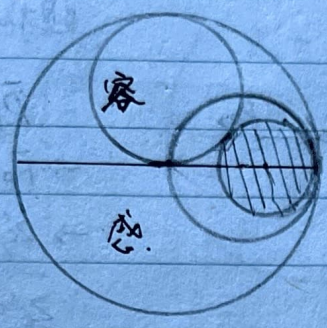
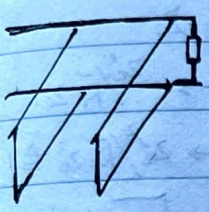


导纳圆图:



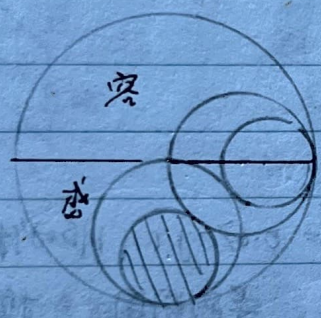
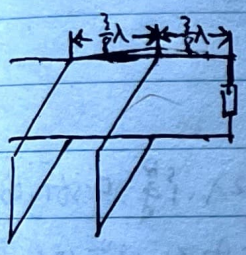
① 求解盲区

P49 例 2.9. (双线圈配电网盲区)

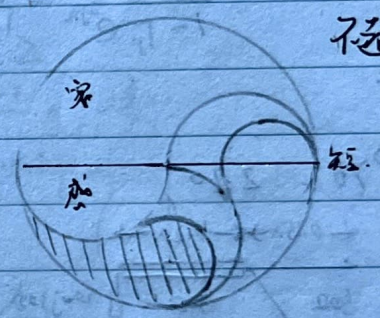


导纳圆图.

P76. 2.11



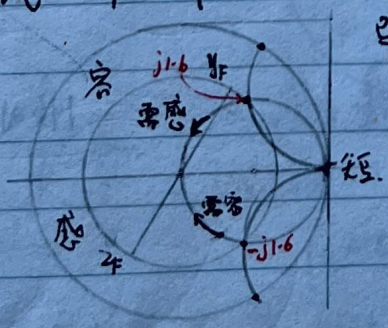
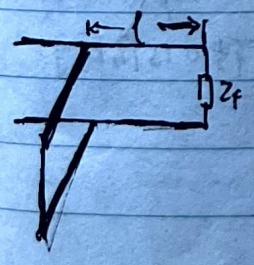
导纳圆图.



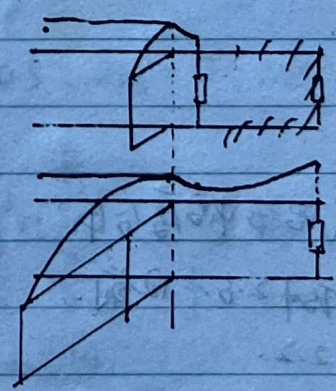
短路

② 单线圈配器

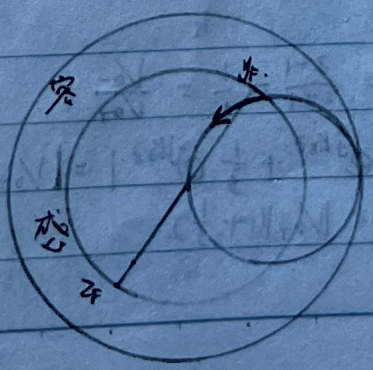
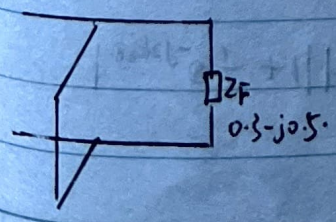
P46 例 2.6. (线上电压分布)



导纳圆图



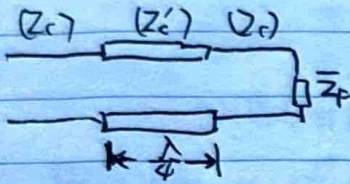
P75. 2.5.



导纳圆图

3. 查图例题

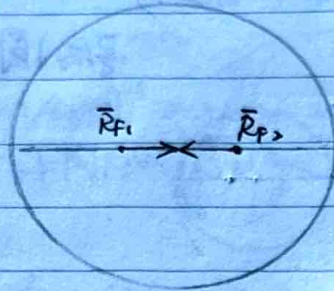
P48. 例 2.8 (4 变压器)



$$Z_i = \frac{1 + \Gamma}{1 - \Gamma} = \frac{1 + \Gamma_F e^{-j2k_0 l}}{1 - \Gamma_F e^{j2k_0 l}}$$

$$= \frac{1 + \Gamma_F e^{-j\pi}}{1 - \Gamma_F e^{j\pi}} = \frac{1 + \Gamma_F}{1 - \Gamma_F} = \frac{1}{Z_F}$$

阻抗圆图



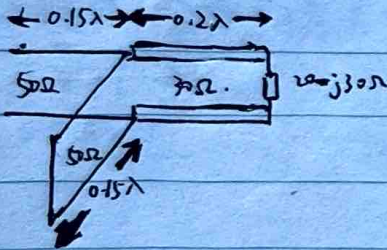
$$\bar{R}_F \rightarrow \bar{R}_F \cdot Z_0$$

$$\rightarrow \bar{R}_F \cdot Z_0 / Z_0' \rightarrow Z_0' / \bar{R}_F \cdot Z_0$$

$$\rightarrow Z_0'^2 / \bar{R}_F Z_0 \rightarrow Z_0'^2 / \bar{R}_F Z_0^2 \cong 1$$

$$\therefore Z_0' = \sqrt{\bar{R}_F Z_0^2} = \sqrt{\bar{R}_F} Z_0$$

P76. 2.10.



$$\Sigma_F = \frac{Z_0 - j30}{Z_0} = 0.67 - j1, \text{ 顺时针转 } 0.2\lambda, \text{ 得 } 0.36 + j0.37$$

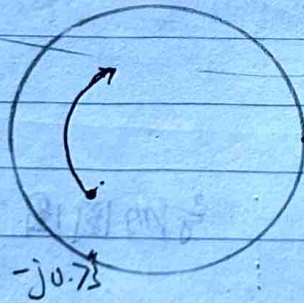
导纳圆图. 按 30 欧姆化, 得 10.8 + j10.8

按 50 欧姆化, 得 0.216 + j0.208

再移后: ~~0.216 + j0.208 - j0.73~~

$$= 0.216 - j0.526$$

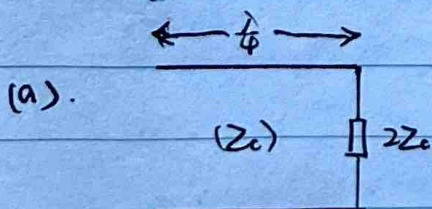
1/4 顺时针转 0.15λ 即可.



4. 画沿线电压幅度分布.

P46 例 2.6. 见前.

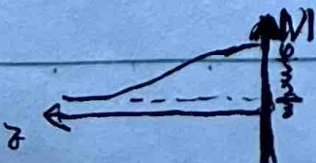
P75 2.2.

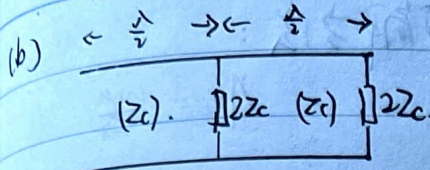


$$\Gamma_F = \frac{Z_L - Z_0}{Z_L + Z_0} = \frac{2Z_0 - Z_0}{2Z_0 + Z_0} = \frac{1}{3} = \frac{V_0^-}{V_0^+}$$

$$\therefore |V| = |V_0^+| |e^{jk_0 z} + \frac{1}{3} e^{-jk_0 z}| = |V_0^+| |1 + \frac{1}{3} e^{-j2k_0 z}|$$

$$z=0 \text{ 时, } |V| = |V_0^+| (1 + \frac{1}{3})$$

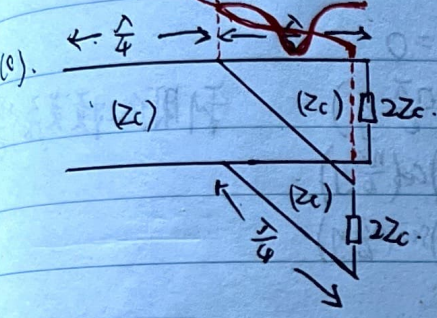
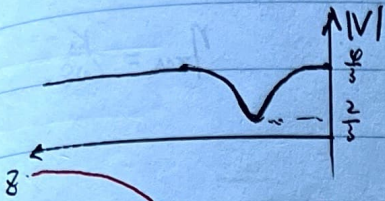




$$\Gamma = \frac{2-1}{2+1} = \frac{1}{3} \quad |V| = |V_{0+}| \left| 1 + \frac{1}{3} e^{jk_0 z} \right|$$

$$Z'_0 = \frac{1-\Gamma}{1+\Gamma} = \frac{1 - \frac{1}{3} e^{-j2k_0 \cdot \frac{\lambda}{4}}}{1 + \frac{1}{3} e^{j2k_0 \cdot \frac{\lambda}{4}}} = \frac{1-\Gamma}{1+\Gamma} = 2Z_0$$

$$\therefore Z_{in} = 2Z_0 \parallel 2Z_0 = Z_0 \quad \therefore \Gamma_{in} = 0$$



$$\Gamma_L = \frac{1}{3}, \quad \Gamma_T = \frac{1}{3}$$

$$Z_{in} = 2Z_0 \parallel \frac{1}{2}Z_0 = \frac{2}{3}Z_0$$

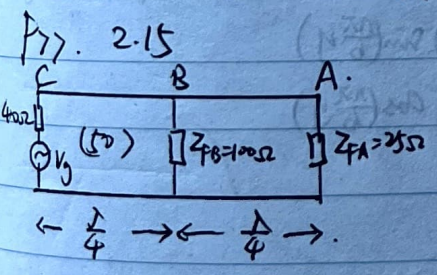
$$\therefore \Gamma_{in} = \frac{\frac{2}{3}-1}{\frac{2}{3}+1} = -\frac{1}{5}$$

$$\therefore |V| = |V_{0+}| \left| 1 - \frac{1}{5} e^{-j2k_0 z} \right|$$

5. 入射波电压, 反射波电压, 总电压, 反射系数的概念

$$V = V_+ + V_-$$

$$\Gamma = \frac{V_-}{V_+}$$



反射系数, $\bar{Z}_{FA} = 0.5, \bar{Z}_{FB} = 2, \therefore \bar{Z}_{in} = 2 \parallel 2 = 1$

$$\therefore \bar{Z}_{in} = 1, \bar{Z}_{in} = 50\Omega$$

$$\therefore \Gamma_C = 0, \dot{V}_B = \dot{V}_g' e^{-jk_0 \cdot \frac{\lambda}{4}} = -j \dot{V}_g', P_{FB} = \frac{V_g'^2}{2R_{FB}}$$

$$\& \bar{Z}_{FA} = 2, \therefore \Gamma_B = \frac{2-1}{2+1} = \frac{1}{3}$$

$$\therefore \dot{V}_- = \frac{1}{3} \dot{V}_B, \dot{V}_+ = \frac{2}{3} \dot{V}_B$$

$$\therefore \dot{V}_A = \dot{V}_- e^{-jk_0 \cdot \frac{\lambda}{4}} + \dot{V}_+ e^{jk_0 \cdot \frac{\lambda}{4}} = (-j \frac{1}{3} + j \frac{2}{3}) \dot{V}_B$$

$$= -j \frac{1}{3} \dot{V}_B = -\frac{1}{2} \dot{V}_g', \quad P_{FA} = \frac{V_g'^2}{8R_{FA}}$$

反射系数的方向性! 瞬时性!

二. 波导

标量波动方程 $\xrightarrow{\text{边界条件}}$ 纵向分量 $\xrightarrow{\text{纵模关系}}$ 横分量

1. 熟悉矩形波导、圆波导、同轴线中场型的求解方法:

矩形、圆: TE:
$$\begin{cases} \nabla_T^2 H_z(x,y) + k_c^2 H_z(x,y) = 0 \\ \frac{\partial H_z}{\partial n} \Big|_{\text{边界}} = 0 \end{cases} \quad \eta_{TE} = \frac{\omega \mu}{k_z}$$

TM:
$$\begin{cases} \nabla_T^2 E_z(x,y) + k_c^2 E_z(x,y) = 0 \\ E_z \Big|_{\text{边界}} = 0 \end{cases} \quad \eta_{TM} = \frac{k_z}{\omega \epsilon}$$

矩形 TE:
$$\begin{cases} \frac{\partial^2}{\partial x^2} H_z + \frac{\partial^2}{\partial y^2} H_z + k_c^2 H_z = 0 \\ \frac{\partial H_z}{\partial x} \Big|_{x=0,a} = 0, \quad \frac{\partial H_z}{\partial y} \Big|_{y=0,b} = 0 \end{cases}$$

$\therefore H_z(x,y) = H_{mn} \cos\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right)$ 利用纵模关系得

$H_x(x,y) = \frac{j k_z}{k_c^2} \left(\frac{m\pi}{a}\right) H_{mn} \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right)$

$H_y(x,y) = \frac{j k_z}{k_c^2} \left(\frac{n\pi}{b}\right) H_{mn} \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right)$

$E_x(x,y) = \eta_{TE} H_y(x,y)$

$E_z(x,y) = -\eta_{TE} H_x(x,y)$

矩形 TM:
$$\begin{cases} \frac{\partial^2}{\partial x^2} E_z + \frac{\partial^2}{\partial y^2} E_z + k_c^2 E_z = 0 \\ E_z \Big|_{x=0,a} = 0, \quad E_z \Big|_{y=0,b} = 0 \end{cases}$$

$\therefore E_z(x,y) = E_{mn} \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right)$ 利用纵模关系得

$E_x(x,y) = -j \frac{k_z}{k_c^2} \left(\frac{m\pi}{a}\right) E_{mn} \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right)$

$E_y(x,y) = -j \frac{k_z}{k_c^2} \left(\frac{n\pi}{b}\right) E_{mn} \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right)$

$H_x(x,y) = -\frac{1}{\eta_{TM}} E_y(x,y)$

$H_y(x,y) = \frac{1}{\eta_{TM}} E_x(x,y)$

圆 TE:
$$\begin{cases} \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial H_z}{\partial r} \right) + \frac{\partial^2 H_z}{\partial \varphi^2} + k_c^2 H_z = 0 \\ \frac{\partial H_z}{\partial r} \Big|_{r=R} = 0 \end{cases}$$

$H_z(r,\varphi) = H_{ni} J_n(k_c r) \cos(n\varphi)$ 利用纵模关系得

$H_r(r,\varphi) = -j \frac{k_z}{k_c^2} H_{ni} J'_n(k_c r) \cos(n\varphi)$

$H_\varphi(r,\varphi) = \frac{j k_z n}{k_c^2 r} H_{ni} J_n(k_c r) \sin(n\varphi)$

$E_r(r,\varphi) = \eta_{TE} H_\varphi(r,\varphi)$

$E_\varphi(r,\varphi) = -\eta_{TE} H_r(r,\varphi)$

同轴TM:

$$\begin{cases} \frac{1}{r} \frac{\partial}{\partial r} (r \frac{\partial E_z}{\partial r}) + \frac{1}{r^2} \frac{\partial^2 E_z}{\partial \varphi^2} + k_c^2 E_z = 0 \\ E_z|_{r=a} = E_z|_{r=b} = 0 \end{cases}$$

$$E_z(r, \varphi) = E_{m0} J_n(k_c r) \cos(n\varphi)$$

利用此法 ---

$$E_r(r, \varphi) = -\frac{j k_c}{k_c} E_{m0} J_n'(k_c r) \cos(n\varphi)$$

$$E_\varphi(r, \varphi) = \frac{j k_c n}{k_c r} E_{m0} J_n(k_c r) \sin(n\varphi)$$

$$H_r(r, \varphi) = -\frac{1}{\eta_{TM}} E_\varphi(r, \varphi)$$

$$H_\varphi(r, \varphi) = \frac{1}{\eta_{TM}} E_r(r, \varphi)$$

同轴线TEM:

$$\nabla_T \cdot \vec{E}(x, y) = 0 \Rightarrow \nabla_T^2 \psi = \frac{1}{r} \frac{\partial}{\partial r} (r \frac{\partial \psi}{\partial r}) + \frac{1}{r^2} \frac{\partial^2 \psi}{\partial \varphi^2} = 0$$

横向无源无旋

$$\Rightarrow \frac{1}{r} \frac{\partial}{\partial r} (r \frac{\partial \psi}{\partial r}) = 0$$

$$\psi = \frac{V}{\ln(a/b)} \ln r$$

$$\vec{E}_T(x, y) = -\frac{\partial \psi}{\partial r} \hat{r} = -\frac{V}{r \ln(a/b)} \hat{r}$$

$$\vec{H}_T(x, y) = \frac{1}{\eta_{TEM}} \hat{z} \times \vec{E}_T(x, y)$$

$$\eta_{TEM} = \frac{\omega \mu}{k} = \sqrt{\frac{\mu}{\epsilon}}$$

$$\gg \gg (\Omega)$$

$$= 120\pi (\Omega)$$

同轴线TE:

$$\begin{cases} \frac{1}{r} \frac{\partial}{\partial r} (r \frac{\partial H_z}{\partial r}) + \frac{1}{r^2} \frac{\partial^2 H_z}{\partial \varphi^2} + k_c^2 H_z = 0 \\ \frac{\partial H_z}{\partial r} |_{r=a} = \frac{\partial H_z}{\partial r} |_{r=b} = 0 \end{cases}$$

同轴线TM:

$$\begin{cases} \frac{1}{r} \frac{\partial}{\partial r} (r \frac{\partial E_z}{\partial r}) + \frac{1}{r^2} \frac{\partial^2 E_z}{\partial \varphi^2} + k_c^2 E_z = 0 \\ E_z|_{r=a} = E_z|_{r=b} = 0 \end{cases}$$

真空

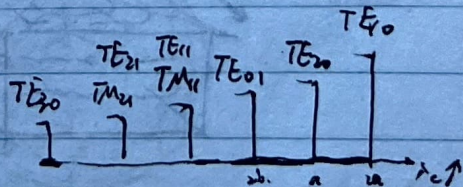
2. 上述3种传输线和波导中各自传输哪一种主模(基模)?

其主模的电磁场分布如何? 怎样才能确保主模的单模传输?

矩形: TE_{10} $\because \lambda_c = 2 / \sqrt{(\frac{m}{a})^2 + (\frac{n}{b})^2}$, $m=1, n=0 \sim m=2, n=0$

\therefore 主模 TE_{10} 的单模传输为 $a < \lambda_c < 2a, \frac{\lambda_c}{2} < a < \lambda_c$

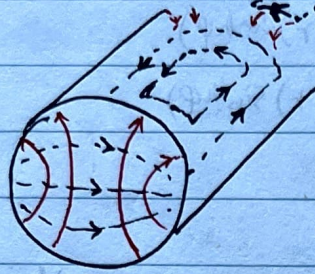
一般2/1频带选为 $1.05a \leq \lambda_c \leq 0.8 \times 2a$



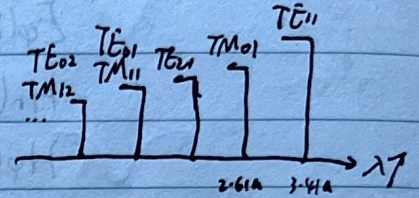
同轴: TE₁₁ $\lambda_c = \frac{2\pi a}{\nu_{ni}}$, $n=1, i=1 \rightarrow TE_{11}$
 $\lambda_c = \frac{2\pi a}{\nu_{ni}}$, $n=0, i=1 \rightarrow TM_{10}$

∴ 主模 TE₁₁ 的单模区为 $2.61a < \lambda_c < 3.41a$

$\frac{\lambda_c}{3.41} < a < \frac{\lambda_c}{2.61}$ $a \approx \frac{\lambda}{3}$



有极化
 简并!
 (n=0时没有)
 无模式简并!

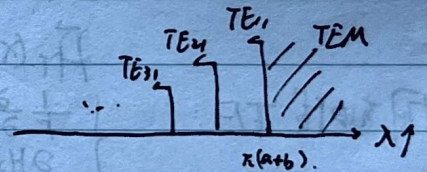
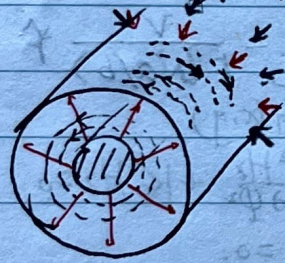


同轴线: TEM⁰ ∴ TE₁₁: $\lambda_c = \pi(a+b)$

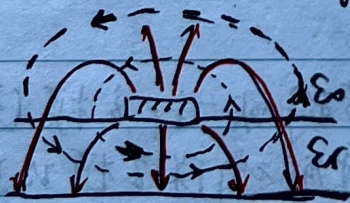
$Z_c = 60 \sqrt{\frac{\mu_r}{\epsilon_r}} \ln(\frac{D}{d})$

∴ 主模 TEM 的单模区为 $\lambda_c \geq \pi(a+b) \Rightarrow \lambda_c \geq 1.1\pi(a+b)$

$\frac{\lambda}{2}(D+d)$

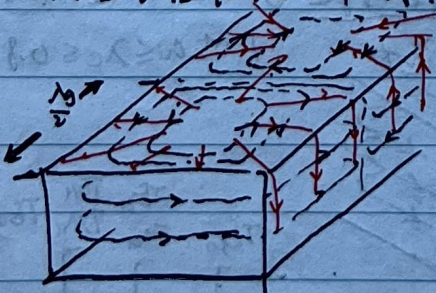


带状线 准 TEM $\lambda_g = \frac{\lambda_0}{\sqrt{\epsilon_c}}$

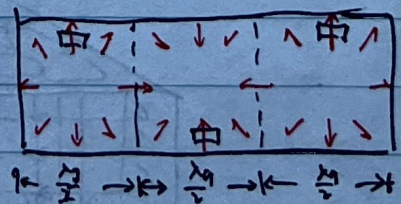


3. TE₀₁ 波的内壁表面电流分布图. 哪些槽缝会切割这些表面电流而引起辐射?

凡向内!



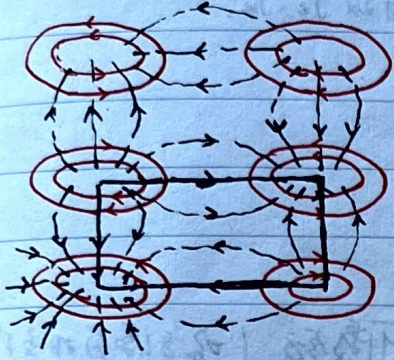
俯视图:



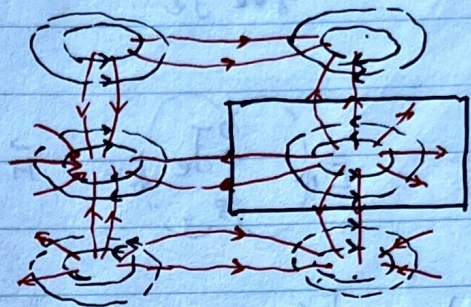
$\left\{ \begin{array}{l} TE \\ TM \end{array} \right.$ E 线图或 H 图型
 TM: H 线图.

4. 矩形波导和圆波导中高阶模的画法.

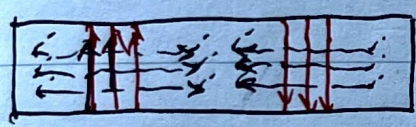
矩形波: TE_{mn}



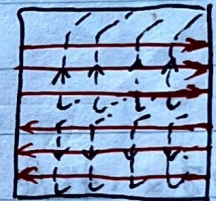
TM_{mn}



圆: TE_{0n} . (场分量在 y 轴均匀分布)

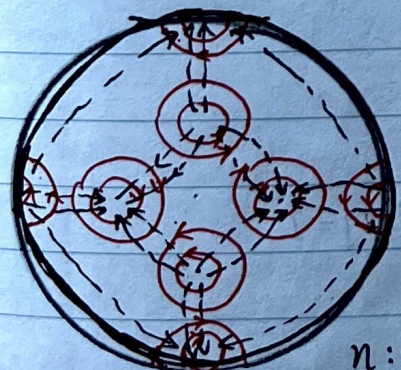


TE_{0n} . (场分量在 x 轴均匀分布)



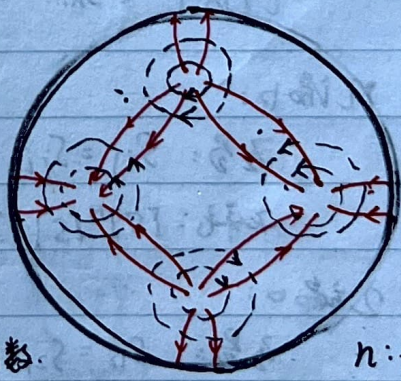
m : 宽边场分量变化的“半周期数”
 n : 窄边场分量变化的“半周期数”.

圆:



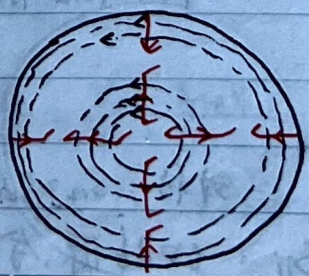
n : 场分量在圆周上变化的周期数.
 i : H_z 分量在 $0 < r < a$ 上的极值数
 (不包括 $r=0$ 处的极值点).

TE_{0i}



n : 场分量在圆周上变化的周期数.
 i : E_z 分量在 $0 < r < a$ 上的零点数
 (不包括 $r=0$ 处的零点).

TM_{0i}

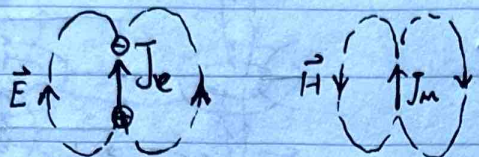


TE_{0i} (场分量在圆周上均匀分布)

TM_{0i} (场分量在圆周上均匀分布)

5. 导体的激励方法与准则.

激励方法: 电场激励、磁场激励、电磁激励
 等效 \vec{J}_e 等效 \vec{J}_m 等效 \vec{J}_e, \vec{J}_m .



激励准则: $\int_V (\vec{E} \cdot \vec{J}_e + \vec{H} \cdot \vec{J}_m) dV \begin{cases} \neq 0 & \text{可激励 (场与源有相互作用)} \\ = 0 & \text{不可激励 (场与源无相互作用)} \end{cases}$
 (条件) 要注意功率守恒条件!

三. 微波网络.

1. 散射参数的定义、性质、物理意义?

定义: $S_{ij} = \frac{b_i}{a_j} |_{a_{k \neq j} = 0}$, 据左式, $S_{ii} = \Gamma_i$

$$\begin{bmatrix} b_1 \\ \vdots \\ b_n \end{bmatrix} = \begin{bmatrix} S_{11} & \cdots & S_{1n} \\ \vdots & \ddots & \vdots \\ S_{n1} & \cdots & S_{nn} \end{bmatrix} \begin{bmatrix} a_1 \\ \vdots \\ a_n \end{bmatrix} \quad \begin{cases} a = I_0 \sqrt{Z_0} = V_0 / \sqrt{Z_0} \\ b = -I_0 \sqrt{Z_0} = -V_0 / \sqrt{Z_0} \end{cases}$$

性质: 几端口:

互易: $S_{ij} = S_{ji}$, $[S] = [S]^T$.

无耗: $[S]^H [S] = I$, \therefore 互易无耗 $[S]^* \cdot [S] = I$

2 端口:

互易: $S_{12} = S_{21}$ (未知)

无耗: $|S_{12}| = |S_{21}|$, $|S_{11}| = |S_{22}|$, $|S_{11}|^2 + |S_{21}|^2 = 1$, $|S_{12}|^2 + |S_{22}|^2 = 1$ (未知)

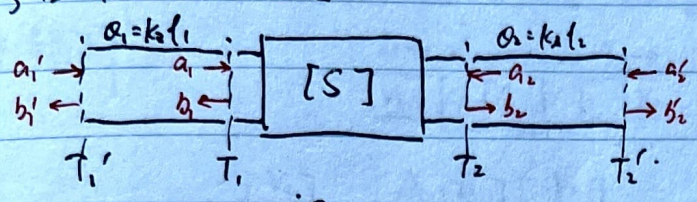
(值: 未知)
 (模: 未知)

对称: $S_{12} = S_{21}$, $S_{11} = S_{22}$ (未知)

物理意义: S_{ii} : i 口接源, 余口接匹配负载, i 口的反射系数.

S_{ij} : j 口接源, 余口接匹配负载, j 至 i 口的电压传输系数.

2. 参考面移动后的[S]



$$S'_{11} = \left. \frac{b_1 e^{-j\theta_1}}{a_1 e^{j\theta_1}} \right|_{a_2=0} = S_{11} e^{-j2\theta_1}$$

$$S'_{22} = \left. \frac{b_2 e^{-j\theta_2}}{a_2 e^{j\theta_2}} \right|_{a_1=0} = S_{22} e^{-j2\theta_2}$$

$$S'_{21} = \left. \frac{b_2 e^{-j\theta_2}}{a_1 e^{j\theta_1}} \right|_{a_2=0} = S_{21} e^{-j(\theta_1+\theta_2)}$$

$$S'_{12} = \left. \frac{b_1 e^{-j\theta_1}}{a_2 e^{j\theta_2}} \right|_{a_1=0} = S_{12} e^{-j(\theta_1+\theta_2)}$$

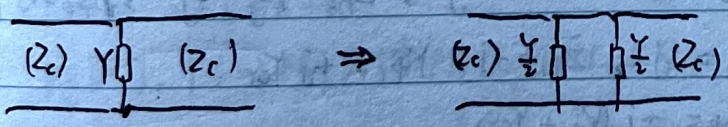
$$\therefore [S'] = \begin{bmatrix} S_{11} e^{-j2\theta_1} & S_{12} e^{-j(\theta_1+\theta_2)} \\ S_{21} e^{-j(\theta_1+\theta_2)} & S_{22} e^{-j2\theta_2} \end{bmatrix} = \begin{bmatrix} e^{j2\theta_1} & 0 \\ 0 & e^{-j2\theta_2} \end{bmatrix} \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} \begin{bmatrix} e^{-j\theta_1} & 0 \\ 0 & e^{-j\theta_2} \end{bmatrix}$$

1端口: $[S'] = [P][S][P]$, $[P] = \text{diag}\{e^{-j\theta_i}\}$, $i=1, \dots, n$.

3. 对称二端口网络[S]的求解方法: 开路 $\rightarrow S_{11}$; 短路 $\rightarrow S_{22}$.

Pr87 例4.5.

$$S_{22} = S_{11} = \frac{S_1 + S_2}{2}, \quad S_{12} = S_{21} = \frac{S_1 - S_2}{2}$$



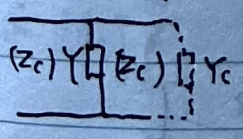
短: $(Z_c) \Rightarrow S_{22} = -1$

开: $(Z_c) \Rightarrow S_{11} = \frac{-Y/2 \cdot Z_c + 1}{+Y/2 \cdot Z_c + 1} = \frac{2Yc - Y}{2Yc + Y}$

$$\therefore S_{11} = S_{22} = \frac{S_1 + S_2}{2} = \frac{1}{2} \cdot \frac{-2Y}{2Yc + Y} = -\frac{Y}{2Yc + Y}$$

$$S_{12} = S_{21} = \frac{S_1 - S_2}{2} = \frac{1}{2} \cdot \frac{4Yc}{2Yc + Y} = \frac{2Yc}{2Yc + Y}$$

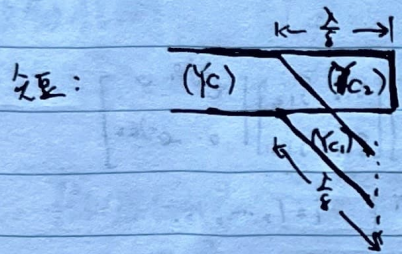
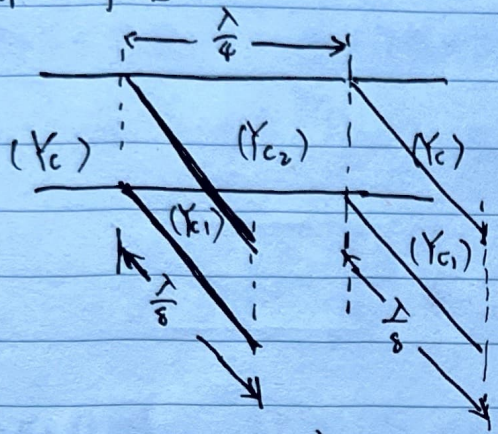
按物理意义求:



$$S_{11} = \left. \frac{b_1}{a_1} \right|_{a_2=0} = \Gamma_1 = \frac{1 - \bar{\gamma}_1}{1 + \bar{\gamma}_1} = \frac{Yc - (Y + Yc)}{Yc + (Y + Yc)} = -\frac{Y}{Y + 2Yc}$$

$$S_{21} = \left. \frac{b_2}{a_1} \right|_{a_2=0} = \frac{a_1 + a_1 \Gamma_1}{a_1} = 1 + \Gamma_1 = \frac{2Yc}{Y + 2Yc}$$

例题



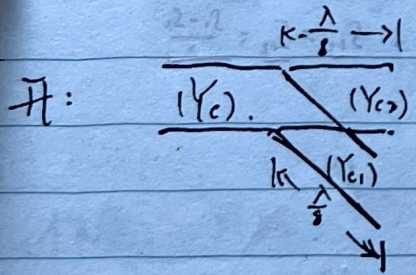
短: $\Gamma_{\phi 2} = -e^{-jk_2 \cdot 2 \cdot \frac{\lambda}{8}} = -(-j) = j, \bar{Z}_{\phi 2} = \frac{1 + \Gamma_{\phi 1}}{1 - \Gamma_{\phi 1}} = \frac{1 + j}{1 - j}$

$\Gamma_{\phi 1} = e^{-jk_2 \cdot \frac{\lambda}{8}} = -j, \bar{Z}_{\phi 1} = \frac{1 + \Gamma_{\phi 2}}{1 - \Gamma_{\phi 2}} = \frac{1 + j}{1 + j}$

$\therefore Z_{\phi 2} = \frac{1}{Y_{c2}} \cdot \frac{1 + j}{1 - j}, Z_{\phi 1} = \frac{1}{Y_{c1}} \cdot \frac{1 + j}{1 + j}$

$\therefore Y_{\phi} = Y_{c2} \frac{1 - j}{1 + j} + Y_{c1} \frac{1 + j}{1 - j}, \bar{Y}_{\phi} = \frac{Y_{c2} \frac{1 - j}{1 + j} + Y_{c1} \frac{1 + j}{1 - j}}{1 + j}$

$\therefore \Gamma_{左} = \frac{1 - \bar{Y}_{\phi}}{1 + \bar{Y}_{\phi}} = \frac{Y_{c1} - (-j Y_{c2} + j Y_{c1})}{Y_{c1} + (-j Y_{c2} + j Y_{c1})} = \frac{Y_{c1} + j(Y_{c1} - Y_{c2})}{Y_{c1} + j(Y_{c1} - Y_{c2})} = S_1$



开: $\Gamma_{\phi 2} = e^{-jk_2 \cdot 2 \cdot \frac{\lambda}{8}} = -j, \bar{Z}_{\phi 2} = \frac{1 + j}{1 - j} = -j, Y_{\phi 2} = +j Y_{c2}$

$\Gamma_{\phi 1} = -j, \bar{Z}_{\phi 1} = -j, Y_{\phi 1} = +j Y_{c1}$

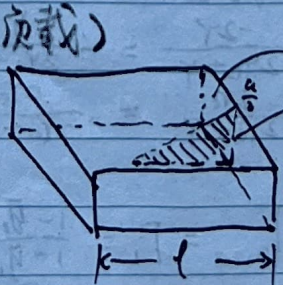
$\therefore Y_{\phi} = +j(Y_{c1} + Y_{c2})$

$\therefore \Gamma_{右} = \frac{Y_{c1} - Y_{\phi}}{Y_{c1} + Y_{\phi}} = \frac{Y_{c1} - j(Y_{c1} + Y_{c2})}{Y_{c1} + j(Y_{c1} + Y_{c2})} = S_2$

$\therefore S_{11} = S_{22} = \frac{S_1 + S_2}{2}, S_{12} = S_{21} = \frac{S_1 \cdot S_2}{2}$

补充题: (单端, TE₀匹配负载)

TE₀/TE₂₀



短路面 (对 TE₂₀)

TE₀匹配负载: $S_{11} = 0$

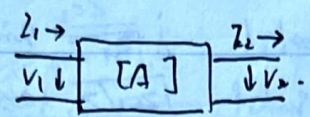
TE₂₀天板: $S_{11} = -e^{-jk_2 l}$

混合 S 矩阵 $[S] = \begin{bmatrix} S^{TE_0, TE_0} & S^{TE_0, TE_{20}} \\ S^{TE_{20}, TE_0} & S^{TE_{20}, TE_{20}} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & -e^{-jk_2 l} \end{bmatrix}$

TE₀输入, 接 TE₀匹配负载时, 输入输出 TE₂₀ / 输入的 TE₁₁

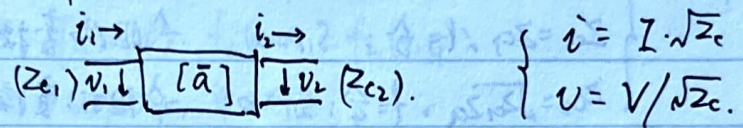
4. 级联矩阵 [A], [a] [a] ~ [S] 的换算.

级联矩阵



$$\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_2 \\ I_2 \end{bmatrix} \quad [A] = \prod_{i=1}^n [A_i]$$

归一化级联矩阵 (转移矩阵).

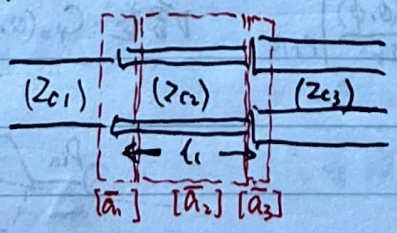


$$\begin{bmatrix} \bar{a} & \bar{b} \\ \bar{c} & \bar{d} \end{bmatrix} = \begin{bmatrix} A \sqrt{\frac{Z_{c2}}{Z_{c1}}} & B / \sqrt{Z_{c1} Z_{c2}} \\ C \sqrt{Z_{c1} Z_{c2}} & D \sqrt{\frac{Z_{c1}}{Z_{c2}}} \end{bmatrix}$$

[a] ~ [S] 的换算:

$$\begin{aligned} S_{11} &= \frac{\bar{a} + \bar{b} - \bar{c} - \bar{d}}{\bar{a} + \bar{b} + \bar{c} + \bar{d}} & \bar{a} &= \frac{1}{2S_{21}} (1 + S_{11} - S_{22} - |S_1|) \\ S_{12} &= \frac{2\bar{b}}{\bar{a} + \bar{b} + \bar{c} + \bar{d}} & \bar{b} &= \frac{1}{2S_{21}} (1 + S_{11} + S_{22} + |S_1|) \\ S_{21} &= \frac{2}{\bar{a} + \bar{b} + \bar{c} + \bar{d}} & \bar{c} &= \frac{1}{2S_{21}} (1 - S_{11} - S_{22} + |S_1|) \\ S_{22} &= \frac{-\bar{a} + \bar{b} - \bar{c} + \bar{d}}{\bar{a} + \bar{b} + \bar{c} + \bar{d}} & \bar{d} &= \frac{1}{2S_{21}} (1 - S_{11} + S_{22} - |S_1|) \end{aligned}$$

例: 求 [a], 何时输入端阻抗匹配 ($S_{11} = \Gamma = 0$)? (1) 用 \bar{a} , 异质用 \bar{A} 方便.



常对 Z_{c1} 归一化 源对 Z_{c3} 归一化.

首先求 $[\bar{a}_2]$:

$$\bar{a} = \frac{V_1}{V_2} \Big|_{I_2=0} = \frac{V_2 \cos k_2 l}{V_2} = \cos k_2 l$$

$$\bar{b} = \frac{V_1}{V_2} \Big|_{I_2=0} = \frac{j 2 V_2 \sin k_2 l}{2 V_2} = j \sin k_2 l$$

∵ 对称 ∴ $\bar{a} = \bar{d}$, $\bar{b} = \bar{c}$.

再求 $[\bar{a}_1]$, 先求 $[A_1]$: (非对称)

$$\bar{A} = \frac{V_1}{V_2} \Big|_{I_2=0} = 1, \quad \bar{B} = \frac{V_1}{V_2} \Big|_{I_2=0} = 0, \quad \bar{C} = \frac{I_1}{V_2} \Big|_{I_2=0} = 0, \quad \bar{D} = \frac{I_1}{V_2} \Big|_{I_2=0} = 1$$

$$\therefore [\bar{a}_1] = \begin{bmatrix} \sqrt{\frac{Z_{c2}}{Z_{c1}}} \bar{A} & \bar{B} / \sqrt{Z_{c1} Z_{c2}} \\ \bar{C} \sqrt{Z_{c1} Z_{c2}} & \bar{D} \sqrt{\frac{Z_{c1}}{Z_{c2}}} \end{bmatrix} = \begin{bmatrix} \sqrt{\frac{Z_{c2}}{Z_{c1}}} & 0 \\ 0 & \sqrt{\frac{Z_{c1}}{Z_{c2}}} \end{bmatrix}$$

另外, $[\bar{a}_3]$ 与 $[\bar{a}_1]$ 类似.

$$\therefore [\bar{a}] = [\bar{a}_1] \cdot [\bar{a}_2] \cdot [\bar{a}_3]$$

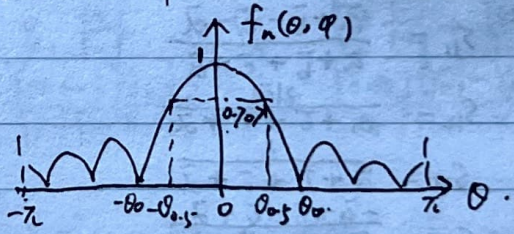
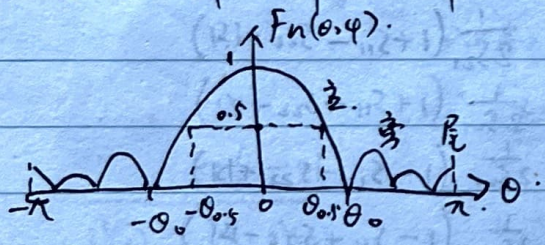
$$= \begin{bmatrix} |Z_{c3}/Z_{c1}| \cos kl & j \sqrt{\frac{Z_{c2}}{Z_{c1} Z_{c3}}} \sin kl \\ \sqrt{\frac{Z_{c3}}{Z_{c1}}} \sin kl & \sqrt{\frac{Z_{c1}}{Z_{c3}}} \cos kl \end{bmatrix}$$

计算出 S_{11} : $S_{11} = \frac{\bar{a} + \bar{b} - \bar{c} - \bar{d}}{\bar{a} + \bar{b} + \bar{c} + \bar{d}} = \frac{1}{k} \left[(\sqrt{\frac{Z_{c2}}{Z_{c1}}} - \sqrt{\frac{Z_{c1}}{Z_{c3}}}) \cos kl + j \left(\frac{Z_{c1}}{\sqrt{Z_{c1} Z_{c3}}} - \sqrt{\frac{Z_{c3}}{Z_{c2}}} \right) \sin kl \right]$
 $(k \neq 0)$

- $Z_{c1} = Z_{c2} = Z_{c3} : S_{11} = 0$ 均匀长线
- $Z_{c1} = Z_{c3}, l = \frac{\lambda}{4} : S_{11} = 0$ $\frac{1}{4}$ 阻抗变换器
- $Z_{c2} = \sqrt{Z_{c1} Z_{c3}}, l = \frac{\lambda}{4} : S_{11} = 0$ $\frac{1}{4}$ 阻抗变换器

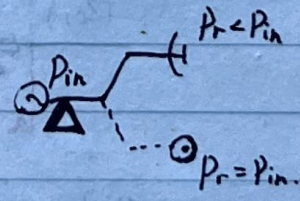
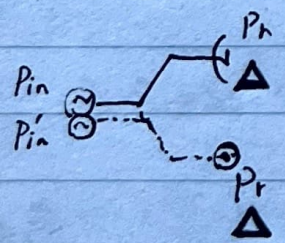
四. 天线

1. 天线方向图中主瓣、旁瓣、尾瓣、半功率角、主瓣零电压张角的含义。



2. 天线方向性系数 D 和增益 G_0 的定义? 它们有何区别?

方向性系数: $D_0(\theta, \phi) = \frac{S_{r, \max}(\theta, \phi)}{P_r / 4\pi r^2} \Big|_{P_r \text{ 同}}$ 增益: $G_0(\theta, \phi) = \frac{S_{r, \max}(\theta, \phi)}{P_r / 4\pi r^2} \Big|_{P_{in \text{ 同}}}$



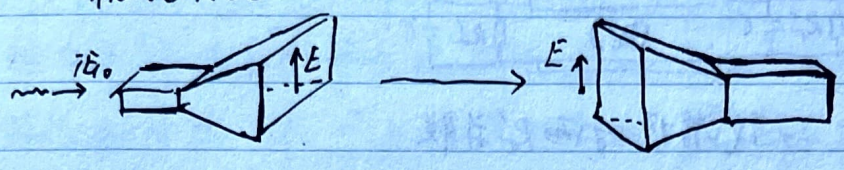
理想天线损耗: $G_0 = D_0$ 一般实际天线: $G_0 < D_0$

3. 何谓天线的极化、极化匹配、极化正交?

- 极化 (最大增益方向) :
- 线极化: 平行 (E 平行于接收端面)、垂直 (垂直于平行极化)
 - 圆极化: 右旋 (右手螺旋)、左旋 (左手螺旋)
 - 椭圆极化: 等于两反旋的等振幅圆极化波的叠加

极化匹配: 收发天线极化一致.

极化正交: 极化失配.

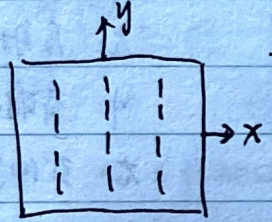


4. 何谓阵列天线的方向图相乘原理? 平面阵列天线的总方向图的分析思路?

$$f_n(\theta, \varphi) = f_a(\theta, \varphi) \cdot f_e(\theta, \varphi) \approx f_a(\theta, \varphi)$$

阵列因子. 单元因子

平面:



先求 $f_{a,y}(\theta, \varphi)$



再求 $f_{a,x}(\theta, \varphi)$

$$\therefore f_n(\theta, \varphi) \approx f_{a,y}(\theta, \varphi) \cdot f_{a,x}(\theta, \varphi)$$

5. 全波振子、半波振子、电偶极子各自的E面和H面方向图(即-1dB场强)?

电偶极子:

$$f_n(\theta) = \sin\theta$$

• E面(即-1dB场强):

半波振子:

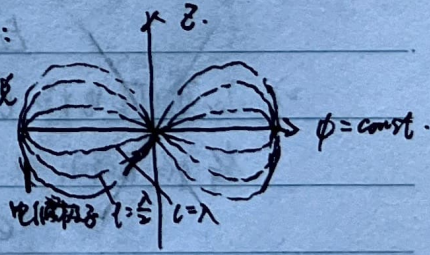
$$f_n(\theta) = \frac{\cos(\frac{\pi}{2} \cos\theta)}{\sin\theta}$$

($c < \lambda$ 时, 越大-波瓣越锐)

全波振子:

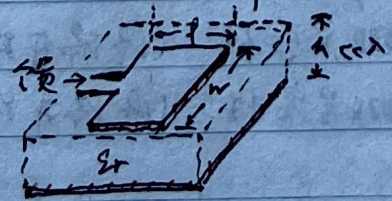
$$f_n(\theta) = \frac{\cos(\pi \cos\theta) + 1}{\sin\theta}$$

• H面(即-1dB): 1图.



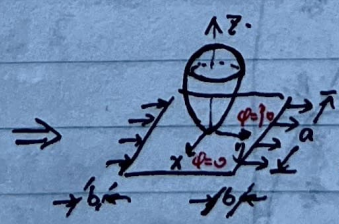
6. 矩形微带天线的结构. 分析方法. 等效电路.

结构:



分析方法:

以矩形微带天线为
单元的二元线阵列
天线.



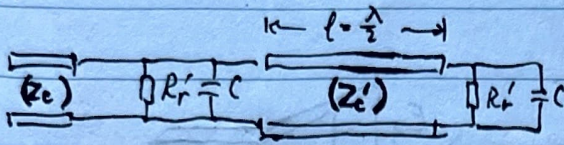
• E面: $\varphi = 90^\circ$ (有 $\frac{kl}{2}$ 波程差)

$$f_{a,E} = S_a \cdot \left(\frac{kl}{2} \sin\theta\right) \cdot 2 \cdot \cos\left(\frac{kl}{2} \sin\theta\right)$$

• H面: $\varphi = 0^\circ$ (无波程差, 加倍)

$$f_{a,H} = S_a \left(\frac{kl}{2} \sin\theta\right) 2 \cdot \cos\theta$$

等效电路:

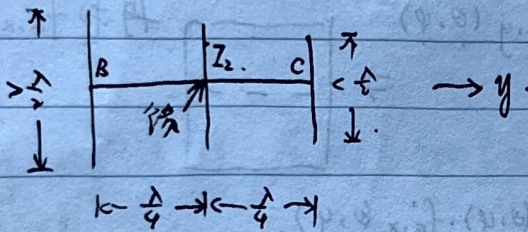
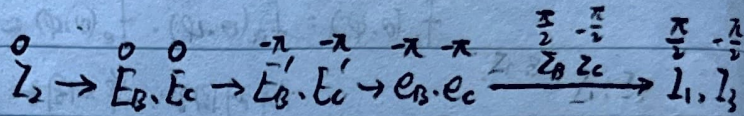


$Z_{in} = R_r/2$. : 天线谐振时两 R_r 并联.

调 R_r : 改变 w

调 λ : 改变 l .

7. 三单元的八木天线的分析方法.



- 左: 反射器
- 中: 有源振子
- 右: 引向器

1) I_2 在 B、C 的辐射场 (近区远场)

$$E_{ac} = jI_2 \frac{e^{-jkR}}{2\pi R} \cdot \frac{\cos(\frac{\pi}{2} \cos \theta)}{R_0} = \frac{2R_0 I_2 \cos(\frac{\pi}{2} \cos \theta)}{\lambda R_0} \quad l = \frac{\lambda}{4}$$

E_b, E_c 与 I_2 同相.

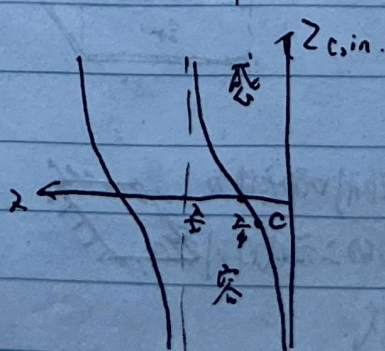
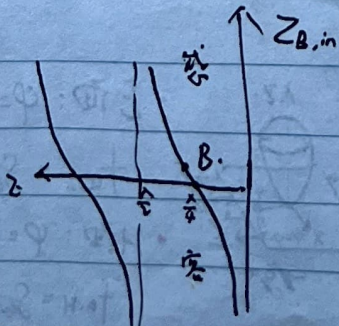
2) I_2 感应电场 $\vec{E}_b, \vec{E}_c \parallel$ 左右两线, 在线内感应出电场 \vec{E}_b', \vec{E}_c' 与 \vec{E}_b, \vec{E}_c 等幅反相

$$e_b = \int_2 \vec{E}_b' \cdot d\vec{l} = - \int_1 \vec{E}_b \cdot d\vec{l}$$

$$e_c = \int_2 \vec{E}_c' \cdot d\vec{l} = - \int_1 \vec{E}_c \cdot d\vec{l}$$

3) 左振子稍长于 $\lambda/4$, B 点输入电阻呈感性 (终端开路)

右振子稍短于 $\lambda/4$, C 点输入电阻呈容性. (终端开路).

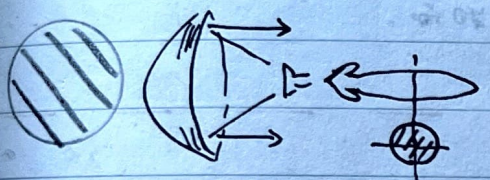


4) 由 $I_B = e_B / Z_{B, in}$, $I_C = e_C / Z_{C, in}$, I_B 领先 I_2 90° , I_2 领先 I_C 90° .
又由近场感应耦合: $I_B \approx I_2 \approx I_C$.

5) 左振子和中振子在 \hat{y} 运场同相叠加, 在 $-\hat{y}$ 反相叠加.
右振子和中振子在 \hat{y} 运场同相叠加, 在 $-\hat{y}$ 反相叠加.

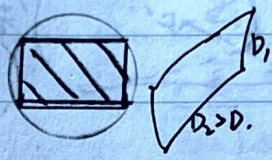
8. 试述几种形式的抛物面天线, 它们产生何种波束, 作何用途?

a) 旋转抛物面天线(圆形面) b) 切割抛物面天线(矩形面)



针状波束

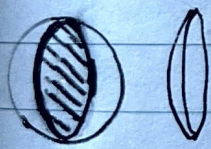
跟踪雷达, 且是地面向站



垂直扇形波束

警戒雷达, 防截站

c) 切割抛物面天线(椭圆形面) d) 抛物柱面天线(矩形面)



水平扇形波束

测高雷达: 通过测仰角, b. 应用



垂直扇形波束

海用导航雷达

9. 对抛物面天线远区场的方法与思路?

口面场法: 由初级波解和抛物面反射特性求焦面上的 E_a, H_a (只存于孔径内)

$$\begin{aligned} H_a E_a &\rightarrow \vec{J}_s, \vec{J}_s \\ &\rightarrow A_m A \rightarrow E, H \end{aligned}$$

由口面源等效原理 & 镜像定理求 \vec{J}_s, \vec{J}_s

由 \vec{J}_s 求 A_m, \vec{J}_s 求 \vec{A} .

由 A_m, \vec{A} 求 E, H .

等效面电流法: 由抛物面反射面内表面的传导电流求远区场, $\vec{J}_s = 2(\hat{n} \times \vec{H}_i)$.

$$\begin{aligned} H_i &\rightarrow \vec{J}_s \\ &\rightarrow \vec{A} \rightarrow E, H \end{aligned}$$

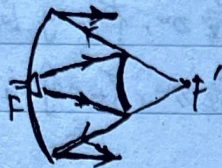
由初级波解特性求 H_i , 即得 \vec{J}_s

由 \vec{J}_s 求 \vec{A} , 积分在口面进行

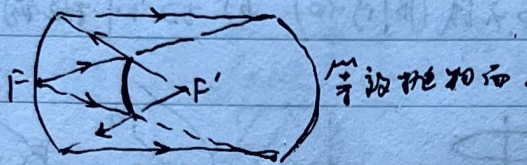
由 \vec{A} 求 E, H .

10. 卡塞格伦天线的两种分析方法.

虚馈源法:(等效馈源法)



等效抛物面法: 给定曲面和抛物面, 只有唯一的一对等效抛物面相对应.



17. 附加

	$2\theta_{05}$	D_0	Z_{in}	R_r	l	E
电波元	90°	1.76dB		$80\pi(\frac{l}{\lambda})^2$	$l \ll \lambda$	
全波振子	47.8°			200Ω	$l = \lambda$	
半波振子	78°	2.15dB	73Ω	73Ω	$l = \frac{\lambda}{2}$	
折叠振子			$2/2\Omega$	146Ω	$l = \frac{\lambda}{4}$	
单极天线	$> 39^\circ$	5.16dB			$l = \frac{\lambda}{4}$	



模式分类:

- 1) 横电波 TE波 H波 磁波 $\eta_{TE} = \frac{c\mu k}{k_z}$
- 2) 横磁波 TM波 E波 电波 $\eta_{TM} = \frac{k_z}{\omega\epsilon}$
- 3) 横电磁波 TEM波 $\eta_{TEM} = \frac{\omega\mu}{k} = \frac{k_z}{\omega\epsilon} = \sqrt{\frac{\mu}{\epsilon}}$ 真空 $120\pi = 377(\Omega)$
- 4) 混合波 EH波 HE波: TE波和TM波的线性组合. e.g. 简并.

模式传播条件:

- | | | |
|----------------------------------------------------------------------------------------------------------------------------------------------------|---|------------------------------------------------------------------------------------------------------------|
| <ol style="list-style-type: none"> 1) 电磁激励方式: 激励与耦合 2) 工作波长: λ 3) 波导尺寸: λ_c | } | <ol style="list-style-type: none"> 1) 激励工作模式, 抑制非工作模式 2) 阻抗匹配 3) 输入能量大小可调 |
|----------------------------------------------------------------------------------------------------------------------------------------------------|---|------------------------------------------------------------------------------------------------------------|

无源微波电路

1. 匹配负载

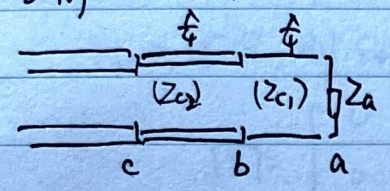
TE₁₀: 平行板: 尖劈形吸收片.

2. 波导接头

TE₁₀: 波导宽壁中位附近有较强 J_z, 容易焊接面.

3. 短路器

S形扼流活塞:



$$\bar{Z}_a = \frac{Z_a}{Z_{c1}}, \quad \bar{Z}_{bz} = \frac{1}{\bar{Z}_a} = \frac{Z_{c1}}{Z_a}, \quad Z_b = \frac{Z_{c1}^2}{Z_a}$$

$$\bar{Z}_{bz} = \frac{Z_{c1}}{Z_a Z_{c2}}, \quad \bar{Z}_{c2} = \frac{1}{\bar{Z}_{bz}} = \frac{Z_a Z_{c2}}{Z_{c1}}, \quad Z_c = \frac{Z_a Z_{c2}^2}{Z_{c1}}$$

当 $Z_a \approx 0$, $(\frac{Z_{c2}}{Z_{c1}})^2 \ll 1$ 时, $Z_c \approx 0$.

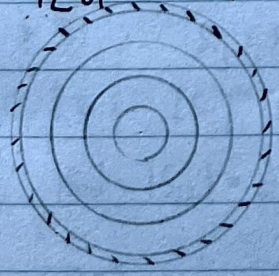
4. 衰减器

旋转极化式衰减器: TE₁₀⁰ → TE₁₁⁰ · cosθ → TE₁₀⁰ · cos²θ

$$[S] = \begin{bmatrix} 0 & \cos^2\theta \\ \cos^2\theta & 0 \end{bmatrix}$$

5. 模式抑制器

TE₀₁⁰ 的抑制器



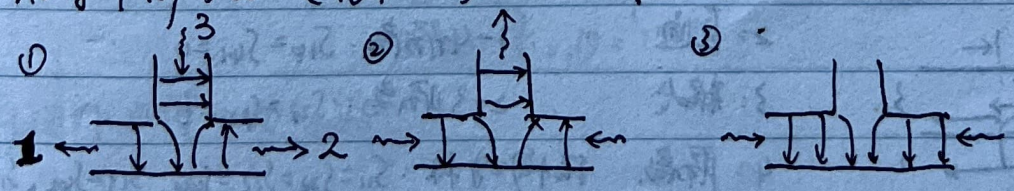
对 TE₁₀⁰:

$$[S] = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$$

对通过模式:

$$[S] = \begin{bmatrix} e^{-jk\ell} & 0 \\ 0 & e^{jk\ell} \end{bmatrix}$$

6. 波导 T 形分支: (无耗互易三端口网络)



对称时: $S_{11} = S_{22}$; 互易: $S_{ij} = S_{ji}$; 结构反时移: $S_{23} = -S_{13}$; 无耗: $[S]^H [S] = I$, 得

$$[S] = \frac{1}{2} \begin{bmatrix} 1 & 1 & \sqrt{2} \\ 1 & 1 & -\sqrt{2} \\ \sqrt{2} & -\sqrt{2} & 0 \end{bmatrix}$$

无耗互易三端口性质:

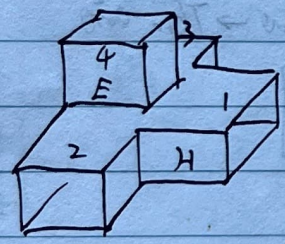
- ① 不可能三端口同时匹配
- ② 不可能两端口同时匹配, 否则退化二端口.

7. 3dB 功率带功分器 (有耗三端口网络).

$$[S] = \begin{bmatrix} 0 & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & 0 & 0 \\ \frac{1}{\sqrt{2}} & 0 & 0 \end{bmatrix}$$

- 1 → 2, 3 : 功分器
- 2, 3 → 1 : 合成器

8. 魔T分支 (无耗互易四端口网络).



结构对称性: $S_{21} = S_{31}, S_{22} = S_{33}$
 $S_{41} = S_{42} = 0, S_{43} = -S_{44}$

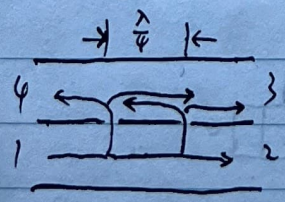
互易性: $S_{ij} = S_{ji}$

1-4 匹配: $S_{11} = S_{44} = 0$

无耗: $[S]^H [S] = I$

$$[S] = \frac{1}{\sqrt{2}} \begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & -1 \\ 0 & 1 & -1 & 0 \end{bmatrix}$$

9. 波导定向耦合器 (无耗互易四端口网络).



2: 直通

3: 耦合

4: 隔离

1-4 隔离: $S_{14} = S_{41} = 0$

2-3 隔离: $S_{23} = S_{32} = 0$

结构对称: $S_{11} = S_{22} = S_{33} = S_{44}, S_{13} = S_{42}, S_{12} = S_{34}$

互易、无耗 ⇒

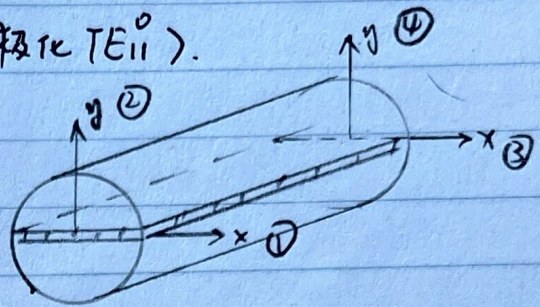
$$[S] = \begin{bmatrix} 0 & S_{12} & S_{13} & 0 \\ S_{12} & 0 & 0 & S_{13} \\ S_{13} & 0 & 0 & S_{12} \\ 0 & S_{13} & S_{12} & 0 \end{bmatrix} \cdot S_{12} \text{ 和 } S_{13} \text{ 相差 } 90^\circ$$

10. 圆极化器: (无耗互易四端口网络)

几何特性上: 二端口
电特性上: 四端口 (水平极化 TE_{11}^0 , 垂直极化 TE_{11}^0)

各端口匹配: $S_{ii} = 0$
正交极化: $S_{12} = S_{14} = S_{23} = S_{34} = 0$

互易: $S_{ij} = S_{ji}$
垂直极化馈入水平极化 $\frac{\pi}{2}$: $S_{31} = e^{-j\varphi}$, 则 $S_{42} = je^{j\varphi}$



$$[S] = \begin{bmatrix} 0 & 0 & e^{-j\varphi} & 0 \\ 0 & 0 & 0 & je^{j\varphi} \\ e^{j\varphi} & 0 & 0 & 0 \\ 0 & je^{-j\varphi} & 0 & 0 \end{bmatrix}$$

11. 旋转对称互端口结: (无耗互易五端口网络)

各端口匹配: $S_{ii} = 0$
旋转对称性: $S_{12} = S_{23} = S_{34} = S_{45} = S_{51} = 0$; $S_{31} = S_{14} = S_{24} = S_{25} = S_{35}$

互易: $S_{ij} = S_{ji}$
无耗: $[S]^H [S] = I_5$

$$\Rightarrow |S_{21}| = |S_{13}| = \frac{1}{2} \quad \text{设 } S_{12} = \frac{1}{2}, S_{13} = \frac{1}{2}e^{j\theta}, \text{ 则}$$

$$S_{13}^* S_{12} + S_{12}^* S_{13} + |S_{12}|^2 = 0$$

$$\frac{1}{4}e^{j\theta} + \frac{1}{4}e^{-j\theta} + \frac{1}{4} = 0$$

$$\cos\theta = -\frac{1}{2}, \theta = 120^\circ$$

可用作四等分功率器。

12. 环流器: (旋转对称无耗互易三端口网络)

$$[S] = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \quad \text{或} \quad \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix} : \text{功率单向循环传输, 反向隔离}$$